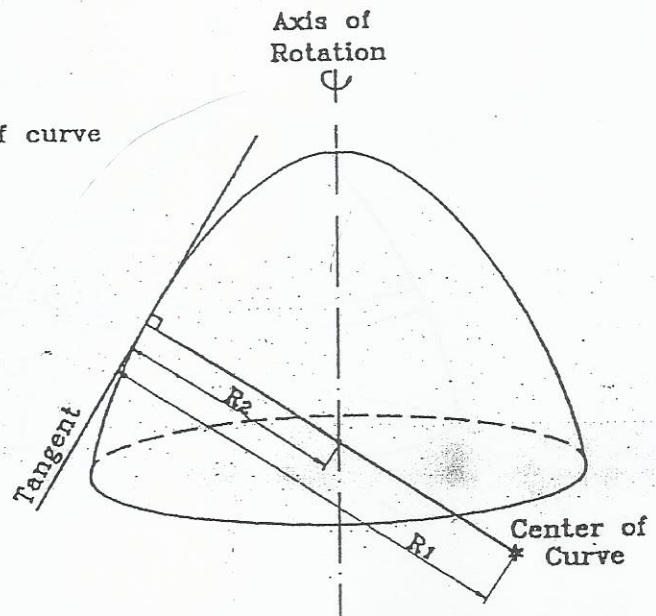


SURFACE OF REVOLUTION

It is surface resulted from rotation of curve around axis of rotation .

R_1 : radius of curve

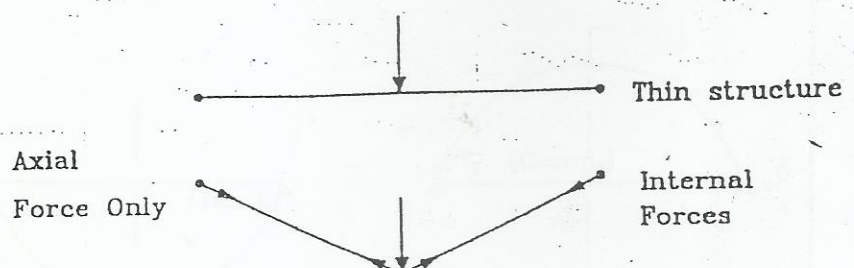
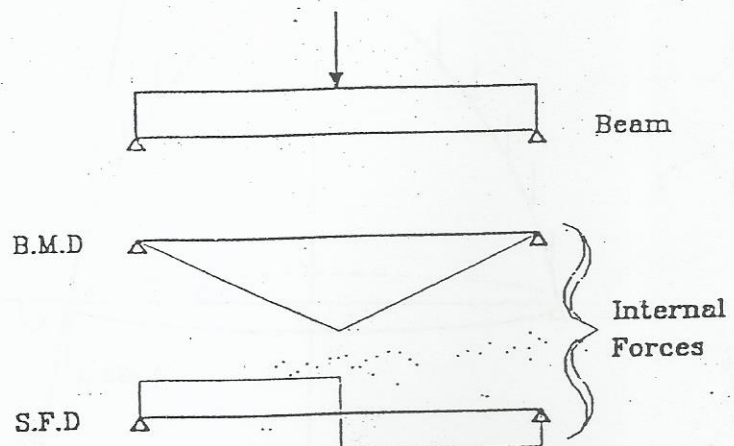
R_2 : Length from tangent to axis of rotation



Membrane theory

For thin structures

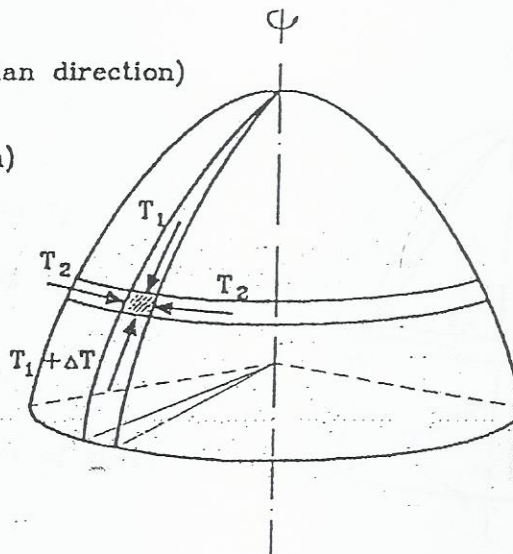
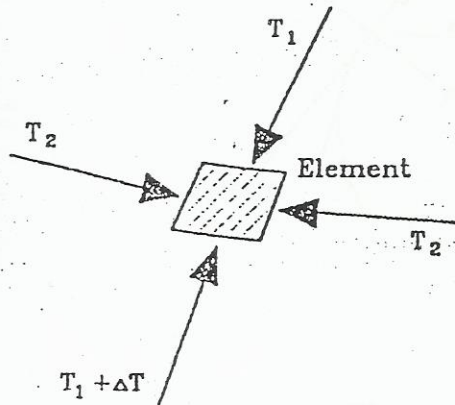
the internal forces are axial force



Internal Forces

T_1 : Meridiane Force (Force in meridian direction)

T_2 : Ring Force (Force in hl direction)



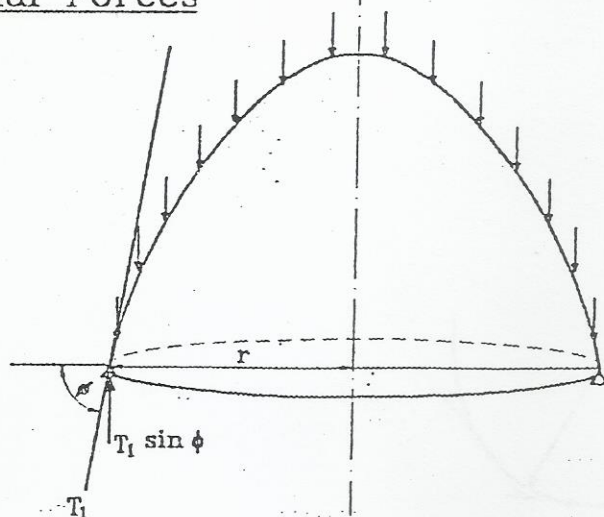
Calculation of Internal Forces

$$\underline{T_1}$$

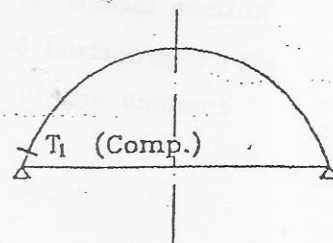
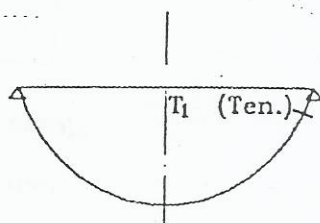
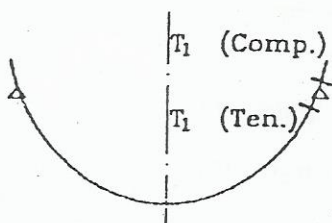
$$\Sigma Y = 0$$

$$W = T_1 \sin \phi$$

$$T_1 = \frac{W \phi}{(\sin \phi) 2 \pi r} \quad \text{t/m}$$



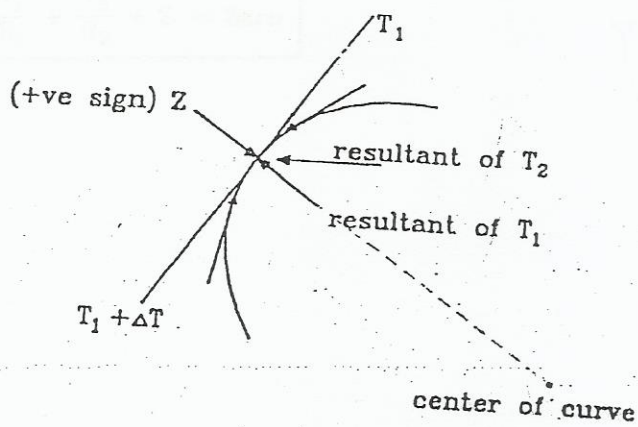
Type of T_1 (Compression or Tension) depends on position of calculated section due to support .



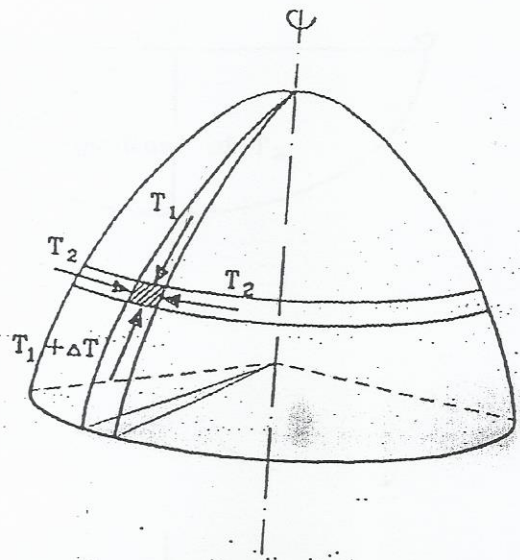
T_1 (Comp.) If calculated section over support

T_2 (Ten.) If calculated section under support

T₂



vertical section
of vertical circle
of the element



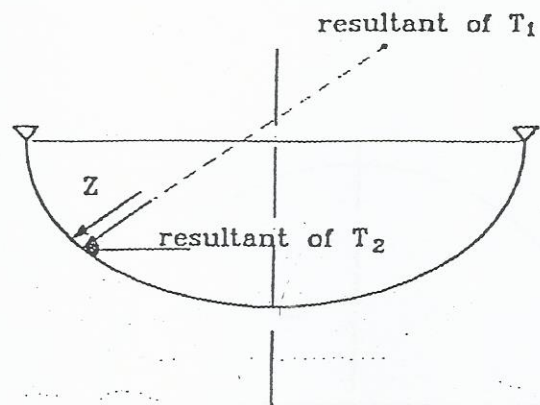
horizontal section
of horizontal circle
of the element

$$\frac{T_1}{R_1} + \frac{T_2}{R_2} = Z$$

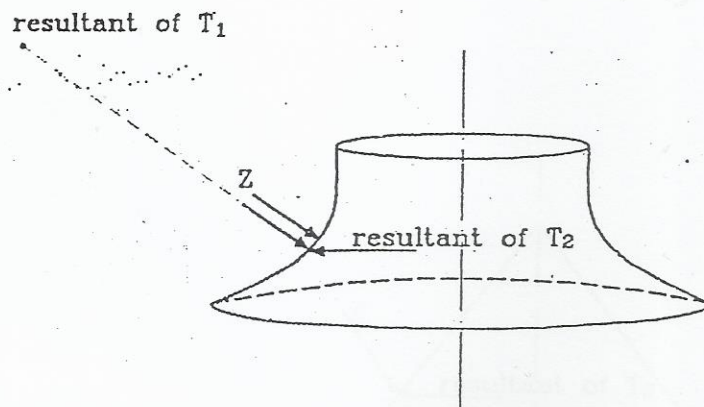
+ve sign means comp.

-ve sign means ten.

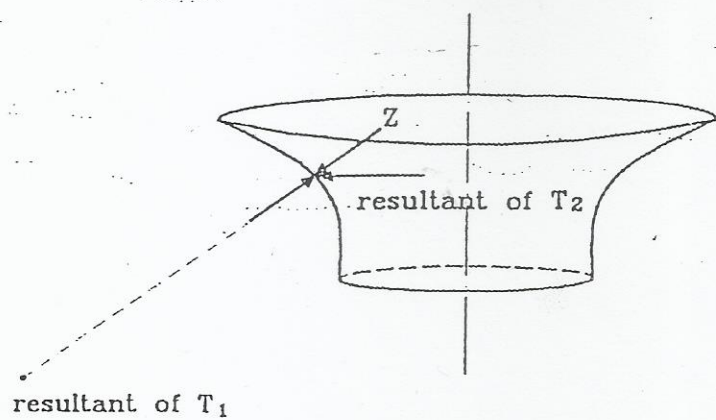
$$\frac{T_1}{R_1} + \frac{T_2}{R_2} + Z = \text{Zero}$$



$$\frac{T_1}{R_1} + Z = \frac{T_2}{R_2}$$



$$\frac{T_1}{R_1} = \frac{T_2}{R_2} + Z$$



Special Cases

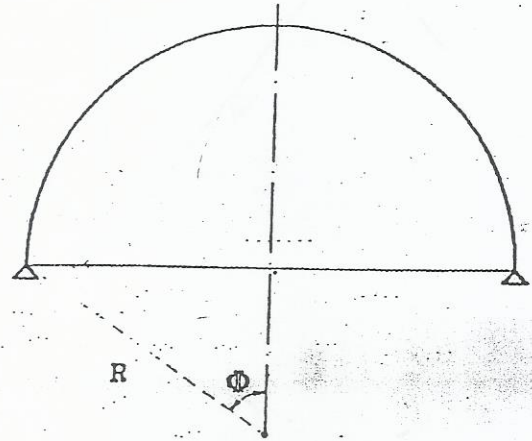
(1) Sphere (Dome)

$$R_1 = R_2 = R$$

where R : radius of the sphere

$$\frac{T_1}{R_1} + \frac{T_2}{R_2} = Z$$

$$T_1 + T_2 = R Z$$



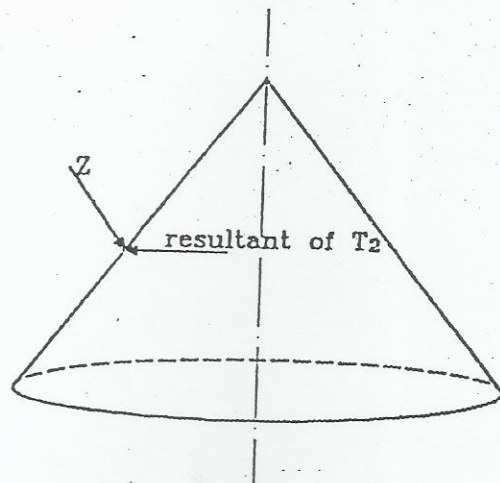
(2) Cone

$$R = \infty$$

$$\frac{T_1}{R_1} = \text{Zero}$$

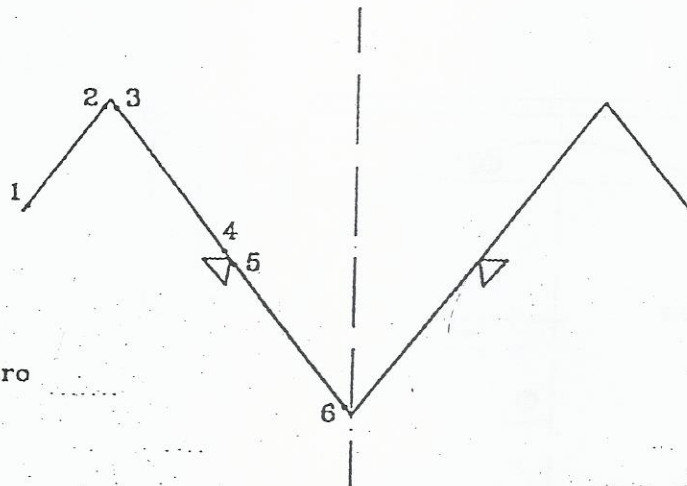
$$\frac{T_2}{R_2} = Z$$

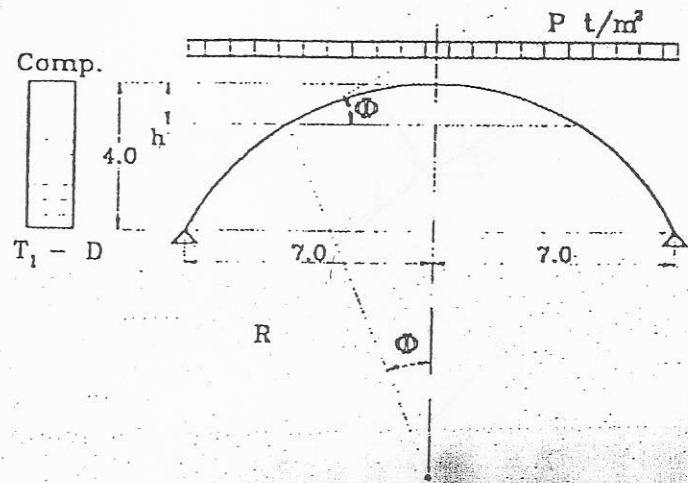
$$T_2 = R_2 Z$$



Example (1)

Determine type of forces
on sections 1---6

sec. (1) $T_1 = \text{Zero}$ $W_\phi = \text{Zero}$ $T_2 = \text{Comp.}$ sec. (2) $T_1 = \text{Ten.}$ $T_2 = \text{Comp.}$ sec. (3) $T_1 = \text{Comp.}$ $T_2 = \text{Ten.}$ sec. (4) $T_1 = \text{Comp.}$ $T_2 = \text{Ten.}$ sec. (5) $T_1 = \text{Ten.}$ $T_2 = \text{Ten.}$ sec. (6) $T_1 = \text{Zero}$ $W_\phi = \text{Zero}$ $T_2 = \text{Zero}$ $R_2 = \text{Zero}$

Example (2)Draw T_1 , T_2 Diagram Due to L.L

$$T_1 = \frac{W_\phi}{2\pi r \sin \phi}$$

$$W_\phi = P (\pi r^2)$$

$$T_1 = \frac{P (\pi r^2)}{2\pi r \sin \phi}$$

$$\sin \phi = \frac{r}{R}$$

$$T_1 = \frac{P (\pi r^2)}{2\pi r \frac{r}{R}} = \frac{P R}{2}$$

$$T_1 + T_2 = R Z$$

$$T_2 = R Z - T_1$$

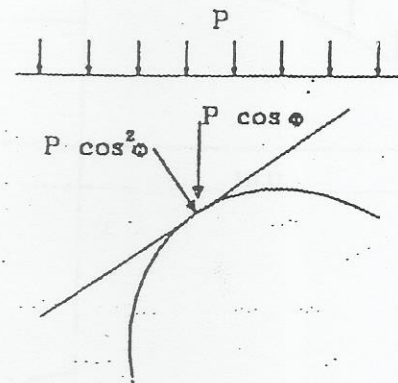
$$T_2 = R P \cos^2 \phi - \frac{P R}{2}$$

$$T_2 = P R \left(\cos^2 \phi - \frac{1}{2} \right)$$

$$R^2 = (7)^2 + (R - 4)^2$$

$$= 49 + R^2 - 8R + 16$$

$$R = 8.125 \text{ m}$$

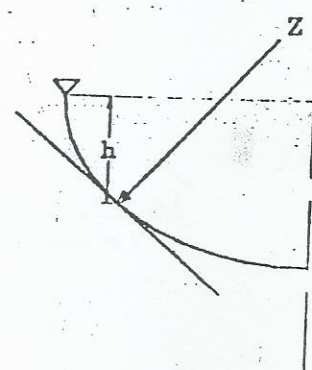
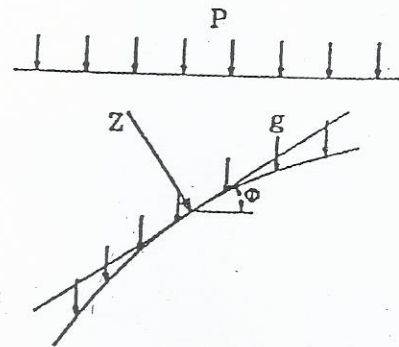


Calculation of Z

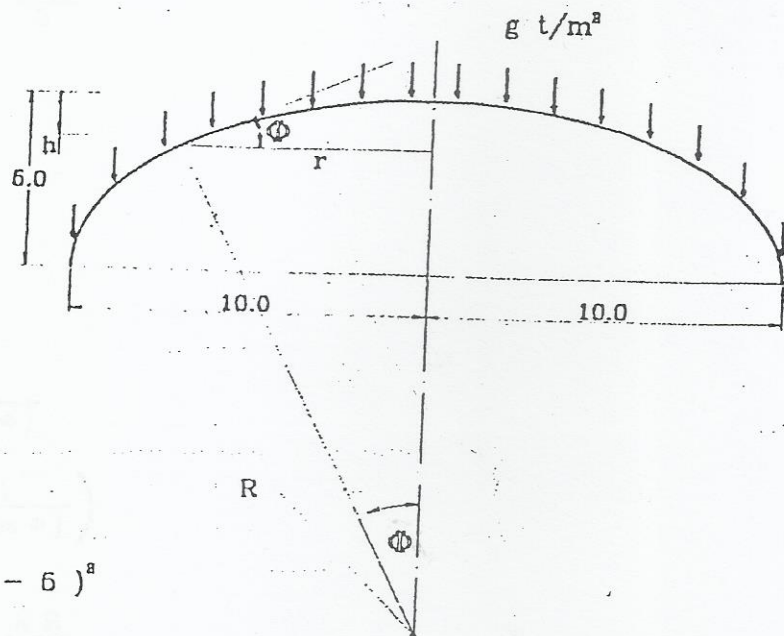
Z is the component of loads perpendicular to the tangent at certain point

$$Z = g \cos \phi + P \cos^2 \phi$$

$$Z = \gamma h + g \cos \phi$$

Example (3)

Draw T_1 , T_2 Diagram



$$\begin{aligned} R^2 &= (10)^2 + (R - 6)^2 \\ &= 100 + R^2 - 10R + 25 \end{aligned}$$

$$R = 12.5 \text{ m}$$

$$W_{\phi} = g \cdot \text{surface area}$$

$$W_{\phi} = g \cdot 2 \pi R h$$

$$T_1 = \frac{W_{\phi}}{2 \pi r \sin \phi}$$

$$T_1 = \frac{g \cdot 2 \pi R h}{2 \pi r \sin \phi}$$

$$\sin \phi = \frac{r}{R}$$

$$h = R - R \cos \phi$$

$$r = R \sin \phi$$

$$h = R (1 - \cos \phi)$$

$$\begin{aligned} T_1 &= \frac{g R R (1 - \cos \phi)}{R \sin \phi \cdot \sin \phi} = \frac{g R (1 - \cos \phi)}{\sin^2 \phi} = \frac{g R (1 - \cos \phi)}{(1 - \cos^2 \phi)} \\ &= \frac{g R (1 - \cos \phi)}{(1 - \cos \phi)(1 + \cos \phi)} = \frac{g R}{(1 + \cos \phi)} \quad \text{t/m} \end{aligned}$$

$$\text{at } \phi = \text{zero} \quad T_1 = \frac{g R}{2}$$

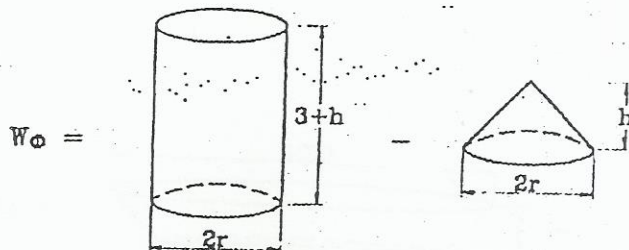
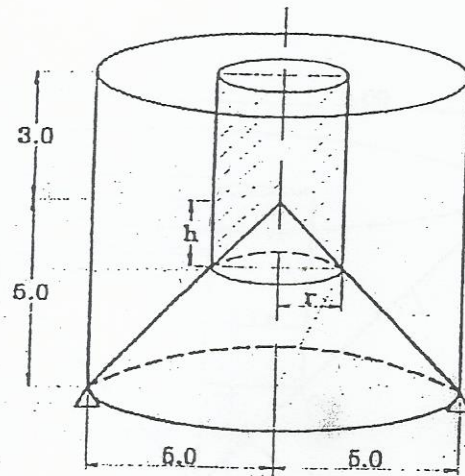
$$T_1 + T_2 = R Z$$

$$T_2 = R Z - T_1$$

$$Z = g \cos \phi$$

$$\begin{aligned} T_2 &= R g \cos \phi - \frac{g R}{(1 + \cos \phi)} \\ &= R g \left(\cos \phi - \frac{1}{(1 + \cos \phi)} \right) \end{aligned}$$

$$\text{at } \phi = \text{zero} \quad T_2 = \frac{g R}{2}$$

Example (4)Calculate T_1 , T_2 for the Cone

$$W_{\phi} = \pi r^2(3+h) - \frac{1}{3}\pi r^2(h)$$

$$T_1 = \frac{W_{\phi}}{2\pi r \sin \phi}$$

 ϕ is constant

$$\tan \phi = \frac{h}{r}$$

$$T_2 = R_2 Z$$

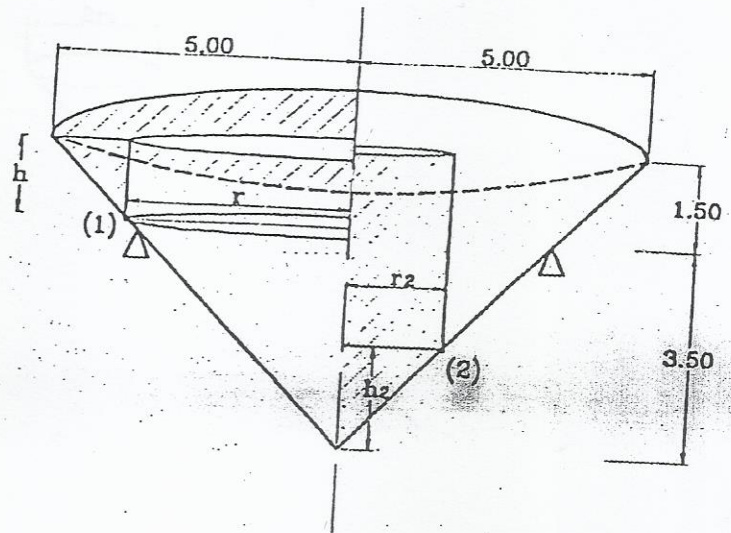
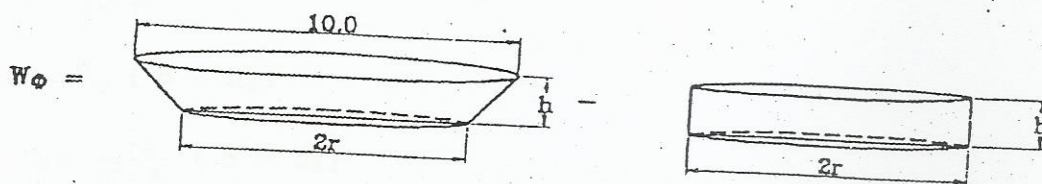
$$R_2 = \frac{r}{\sin \phi}$$

$$Z = \gamma_w (h + 3)$$

$$T_2 = \frac{r}{\sin \phi} (h + 3)$$

Example (5)

Calculate T_1 , T_2 for the Cone
full of water

sec..(1)

$$T_1 = \frac{W_\phi}{2\pi r \sin \phi}$$

$$T_2 = R_2 Z$$

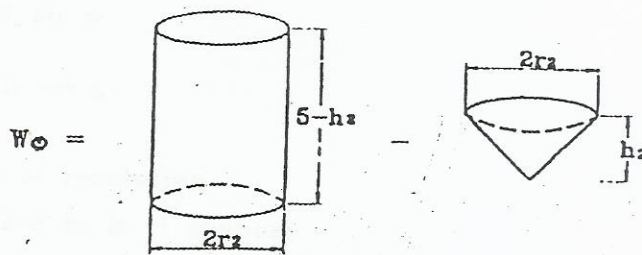
$$R_2 = \frac{r}{\sin \phi}$$

$$Z = \gamma_w h$$

$$W_\phi = \text{Area of triangle} \cdot \text{Perimeter of c.g. circle}$$

$$= \left(\frac{5-r}{2} \cdot h \right) \cdot 2 \left(r + \frac{5-r}{3} \right)$$

sec. (2)



$$W_{\phi} = \pi r_2^2 (5 - h_2) + \frac{1}{3} \pi r_2^2 (h_2)$$

$$T_1 = \frac{W_{\phi}}{2 \pi r_2 \sin \phi}$$

$$T_2 = R_2 Z$$

$$R_2 = \frac{r_2}{\sin \phi}$$

$$Z = \gamma_w (5 - h_2)$$

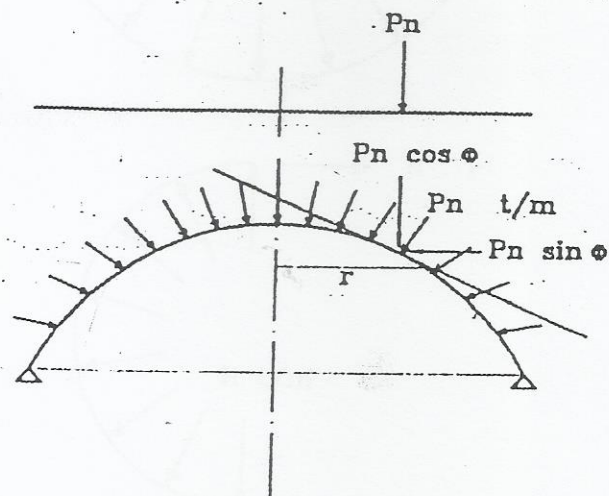
$$T_2 = \frac{r_2}{\sin \phi} (5 - h_2)$$

- W_{ϕ} for case of load perpendicular to the tangent

$$W_{\phi} = P_n \cdot \text{area of } hL \text{ projection}$$

$$= P_n \cdot \pi r^2$$

$$Z = P_n$$

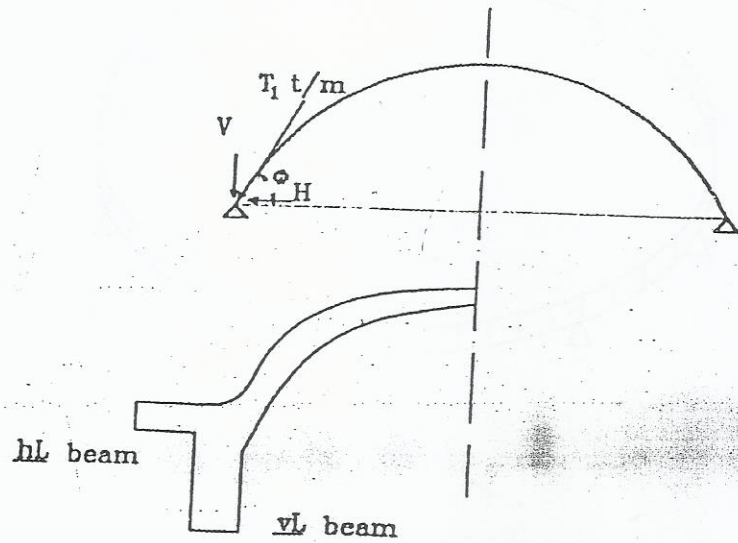


supports of surface of revolution

$$V = T_1 \sin \phi$$

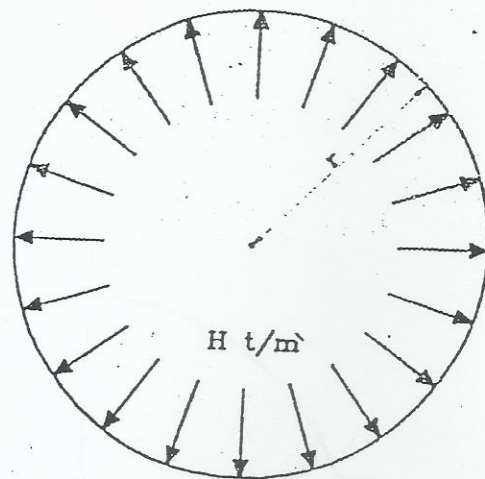
$$H = T_1 \cos \phi$$

Surface of revolution
must have hl & vl support

(1) hL beam

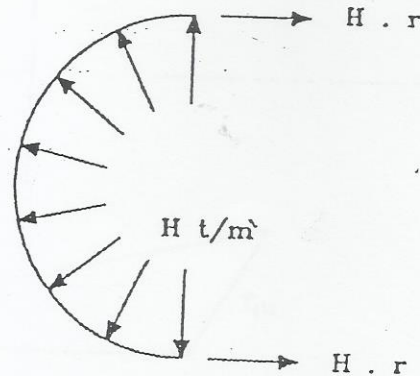
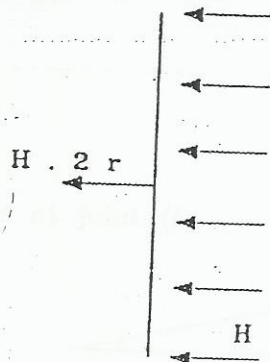
Internal Force is Axial Force

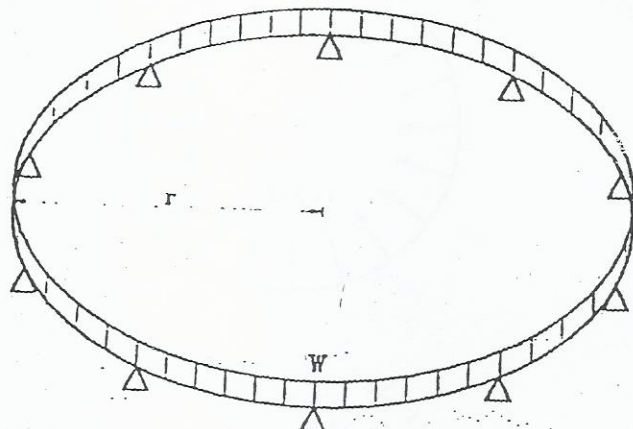
$$\text{Axial Force} = H \cdot r \quad \text{Tension}$$



$$A_s = \frac{T_u}{\frac{F_y}{\gamma_s}}$$

$$A_c = (30 - 50) A_s$$



(2) vL beam

$$w = V + \text{o.w of hL beam}$$

$$+ \text{o.w of vL beam}$$

from tables

$$Q = \dots$$

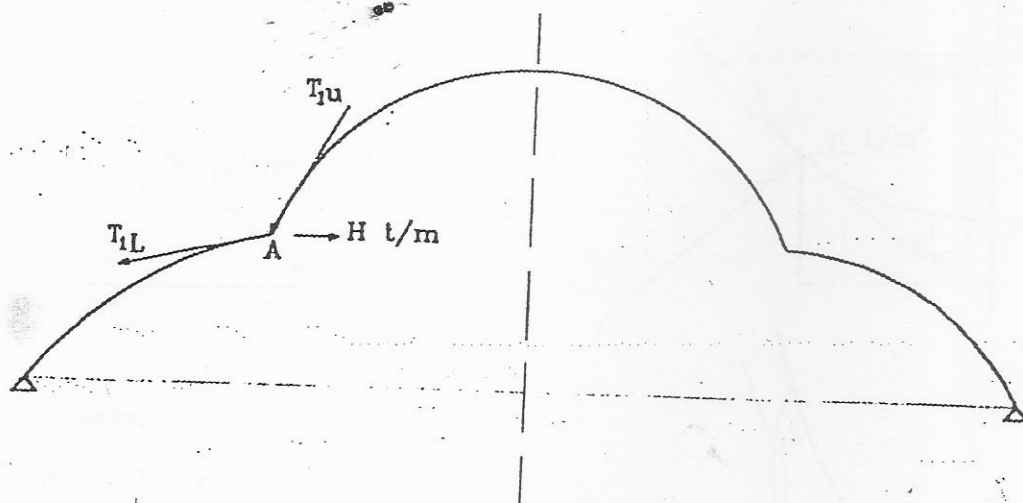
$$\text{B.M (at Mid span)} = \dots$$

$$M_{-ve} \text{ (at support)} = \dots$$

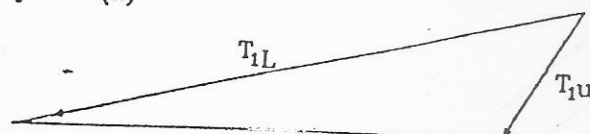
$$M_t = \dots$$

- Surface supported to another

(1)



Triangle of forces at joint (A)



$$\text{Axial Force} = H \cdot r$$

Compression Force

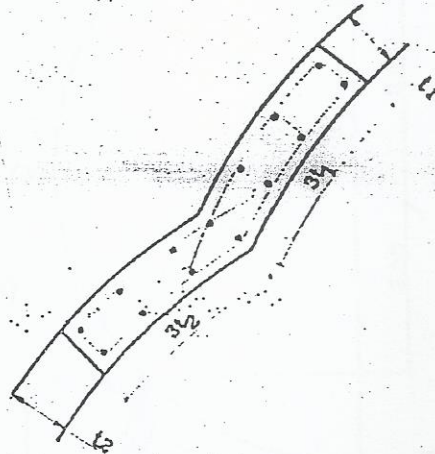
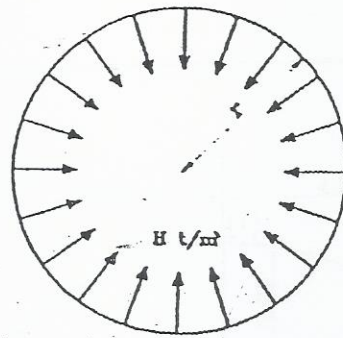
Design equation as column

$$P_u = 0.35 A_c F_{cu} + 0.67 A_s F_y$$

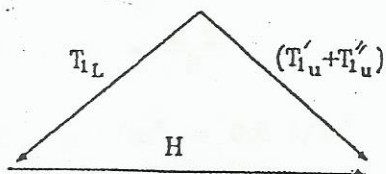
$$\text{assume } A_c = 3 t_1^2 + 3 t_2^2$$

$$\therefore A_s = \dots$$

$$\min (0.8 \% A_c)$$



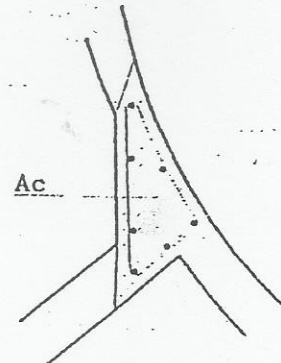
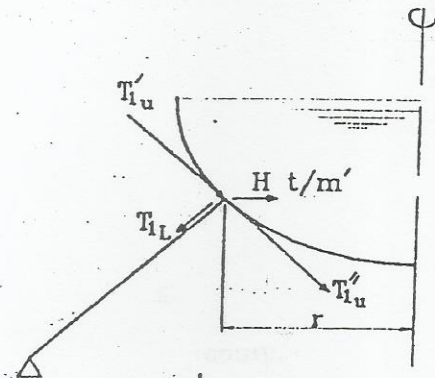
(1)



Compression Force

$$\text{at intersection} = H \cdot r$$

$$P_u = 0.35 A_c F_{cu} + 0.67 A_s F_y$$

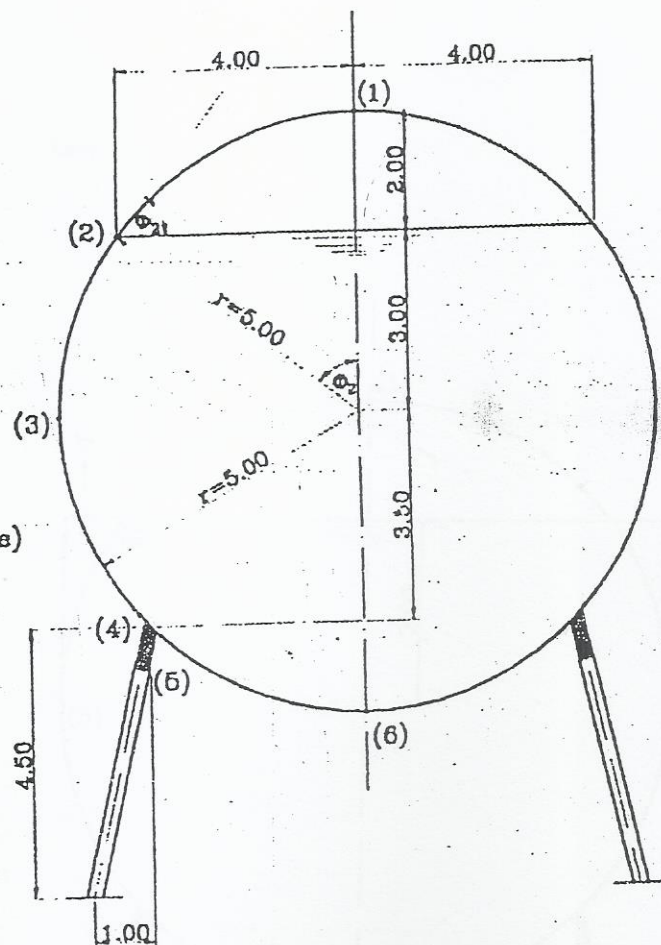


Example (6)

Calculate the internal forces
at the shown sections .

assume $t = 20$ cm (water structure)

o.w of slab = 0.5 t/m²

Sec. (1)

$$T_1 = T_2 = \frac{R Z}{2}$$

$$Z = g t/m^2 = 0.5 \text{ t/m}^2$$

$$T_1 = T_2 = \frac{5 \cdot 0.5}{2} = 1.25 \text{ t/m}^2$$

comp.

Sec. (2)

$$W_\phi = 0.5 \cdot 2\pi \cdot 5 \cdot 2 = 31.42 \text{ t}$$

$$T_1 = \frac{W_\phi}{2\pi r \sin \phi}$$

$$r = 4.0 \quad \phi = \phi_2 = \cos^{-1} \frac{3}{5} = 53.13^\circ$$

$$T_1 = \frac{31.42}{2\pi \cdot 4 \cdot \sin 53.13} = 1.56 \text{ t/m}^2$$

comp.

$$T_1 + T_2 = R Z$$

$$Z = g \cos \phi = 0.3 \text{ t/m}^2$$

$$1.56 + T_2 = 5 \cdot 0.3$$

$$T_2 = -0.08 \text{ t/m}^2$$

ten.

Sec. (3)

$$W_\phi = 0.5 W_{1-3} + W_1$$

$$W_\phi = 0.5 \cdot 2\pi \cdot 5^2 - \left\{ \pi \cdot 5^2 \cdot 3 - \frac{\pi \cdot 3}{6} (3 \cdot 5^2 + 3 \cdot 4^2 + 3^2) \right\} = 50.27 \text{ t}$$

$$T_1 = \frac{W_\phi}{2\pi r \sin \phi}$$

$$r = 5.0$$

$$\phi = 90^\circ$$

$$T_1 = \frac{50.27}{2\pi \cdot 5 \cdot \sin 90} = 1.6 \text{ t/m}$$

comp.

- just before sec. (3)

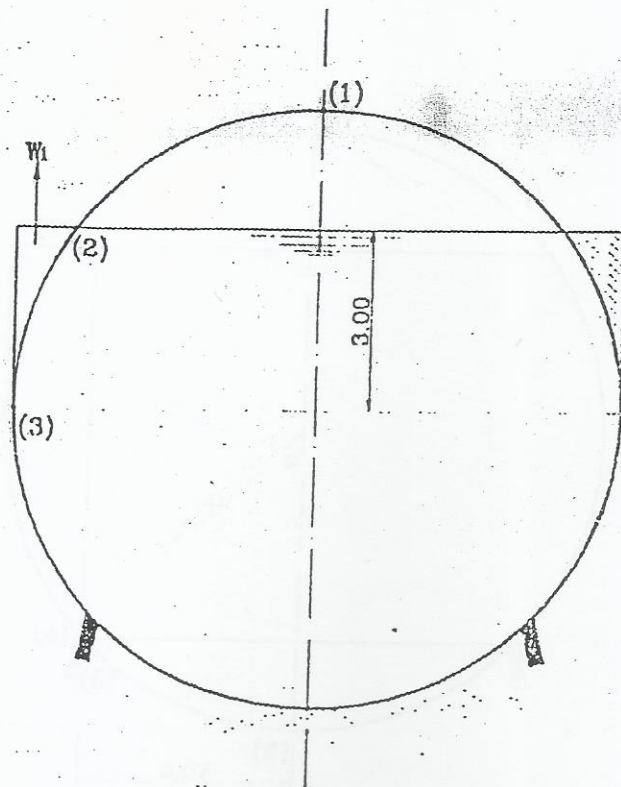
$$T_1 + T_2 = R Z$$

$$Z = \gamma h = 1 \cdot 3 = 3 \text{ t/m}^2$$

$$1.6 + T_2 = 5 \cdot 3$$

$$T_2 = 13.4 \text{ t/m}^2$$

comp.



— just after sec. (3)

$$T_1 + T_2 + R Z = \text{zero}$$

$$Z = \gamma h = 1 \cdot 3 = 3 \text{ t/m}^2$$

$$1.6 + T_2 + 5 \cdot 3 = \text{zero}$$

$$T_2 = -16.6 \text{ t/m}^2$$

Sec. (4)

$$\begin{aligned} W_\phi &= 0.5 \left\{ 2\pi \cdot 5^2 + \right. \\ &\quad \left. + 2\pi \cdot 5 \cdot 3.5^2 \right\} \\ &\quad + \left\{ \frac{\pi \cdot 6.5}{8} (3 \cdot 4^2 + \right. \\ &\quad \left. + 3 \cdot 3.57^2 + 6.5^2) \right. \\ &\quad \left. - \pi \cdot 3.57^2 \cdot 6.5 \right\} \\ &= 310.55 \text{ t} \end{aligned}$$

$$T_1 = \frac{W_\phi}{2\pi r \sin \phi}$$

$$r = 5.0$$

$$\sin \phi = \frac{3.57}{5}$$

$$T_1 = \frac{50.27}{2\pi \cdot 5 \cdot \frac{3.57}{5}} = 19.4 \text{ t/m}$$

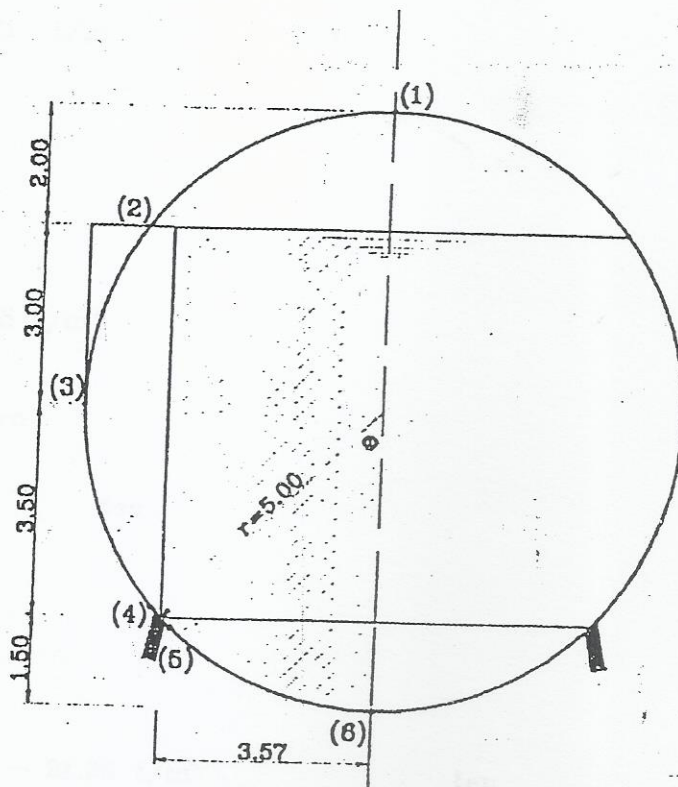
$$T_1 + T_2 + R Z = \text{zero}$$

$$\begin{aligned} Z &= \gamma h + g \cos \phi \\ &= 1 \cdot 6.5 + 0.5 \cos \phi = 6.85 \text{ t/m}^2 \end{aligned}$$

$$19.4 + T_2 + 5 \cdot 6.85 = \text{zero}$$

$$T_2 = -53.65 \text{ t/m}^2$$

len.



comp.

len.

Sec. (5)

$$W\phi = 0.5 \cdot 2\pi \cdot 5 \cdot 1.5 + \pi \cdot 3.57^2 \cdot 8.5 +$$

$$+ \pi \cdot 1.5^2 \cdot \left(5 - \frac{1.5}{3.0}\right) = 315.83 \text{ t}$$

$$T_1 = \frac{W\phi}{2\pi r \sin\phi}$$

$$r = 5.0$$

$$\sin\phi = \frac{3.57}{5}$$

$$T_1 = \frac{315.83}{2\pi \cdot 3.57 \cdot \frac{3.57}{5}} = 19.71 \text{ t/m} \quad \text{ten.}$$

$$T_1 + T_2 + R Z = \text{zero}$$

$$Z = \gamma h + g \cos\phi$$

$$= 1 \cdot 6.5 + 0.5 \cos\phi = 6.85 \text{ t/m}^2$$

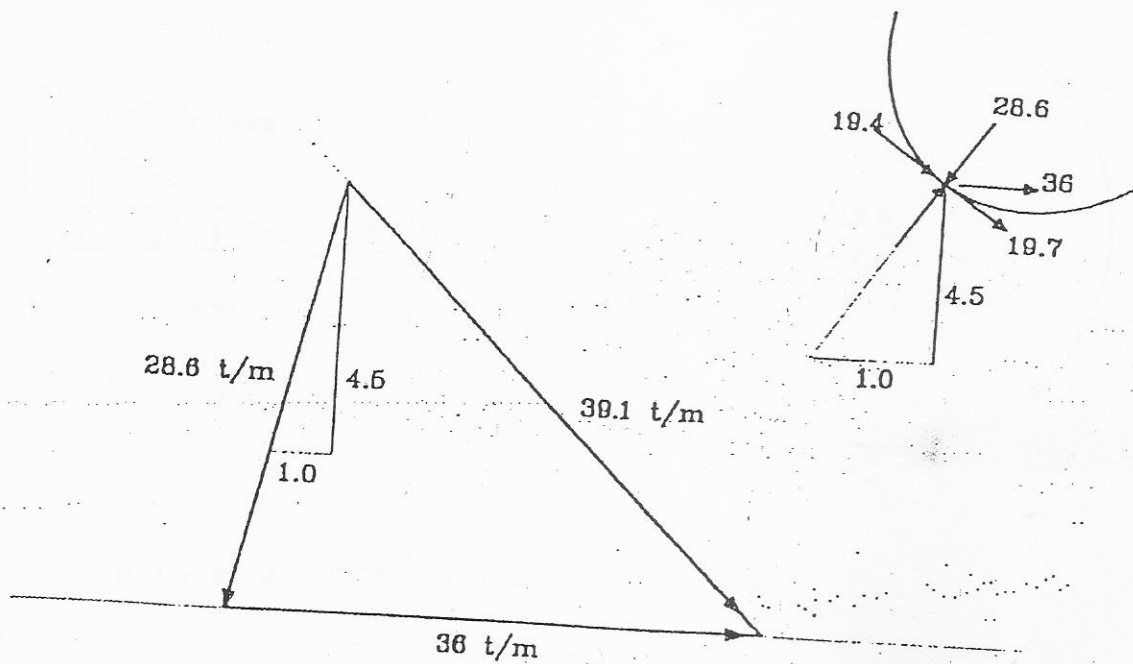
$$-19.71 + T_2 + 5 \cdot 6.85 = \text{zero}$$

$$T_2 = -14.54 \text{ t/m} \quad \text{ten.}$$

Sec. (6)

$$T_1 = T_2 = \frac{R Z}{2}$$

$$= -5 \cdot \frac{(8 + 0.5)}{2} = -21.25 \text{ t/m} \quad \text{ten.}$$

Design of Support

$$w = 28.6 + \text{component of o.w}$$

assume sec. 40×100

$$w = 28.6 + 0.4 \times 1 \times 2.5$$

$$= 29.6 \text{ t/m}$$

$$P = 2\pi \times 3.57 \times 29.6 =$$

$$= 663.96 \text{ ton}$$

assume 6 column

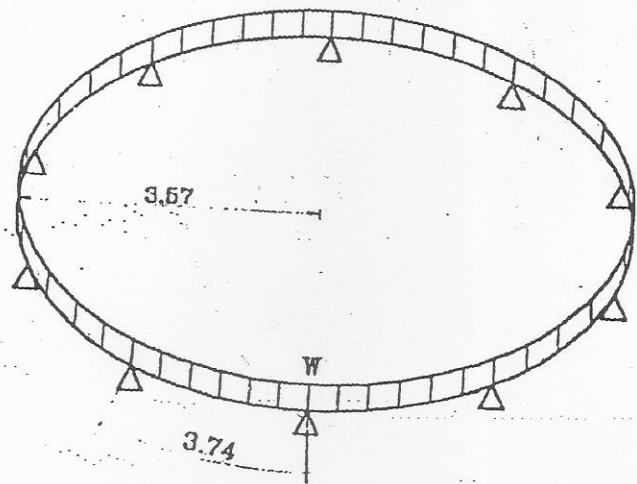
$$\text{Load / col.} = \frac{P}{6} = 110.7 \text{ ton}$$

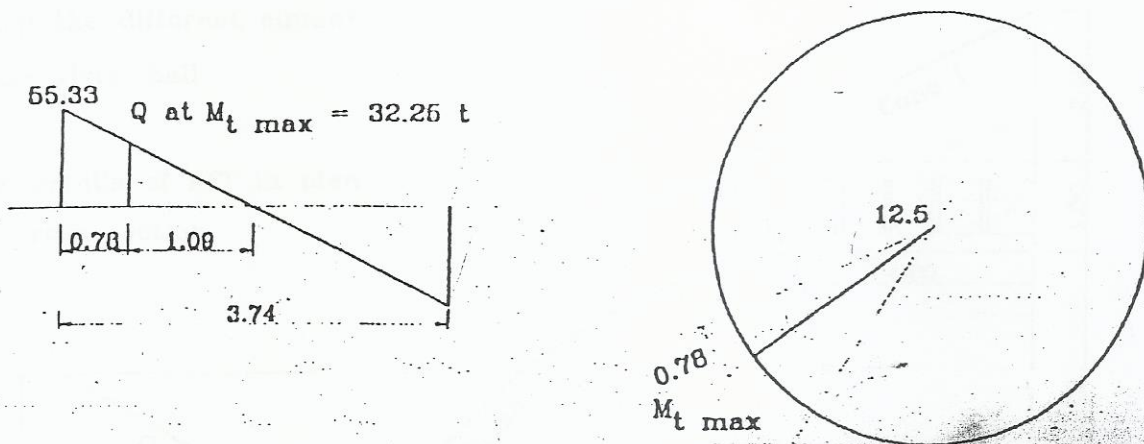
$$Q_{\text{max.}} = \frac{P}{12} = 55.33 \text{ ton}$$

$$M_{+ve} = 0.0075 \times 663.96 \times 3.57 = 17.8 \text{ m.t}$$

$$M_{-ve} = -0.0148 \times 663.96 \times 3.57 = -35.1 \text{ m.t}$$

$$M_t = 0.0015 \times 663.96 \times 3.57 = 3.6 \text{ m.t}$$

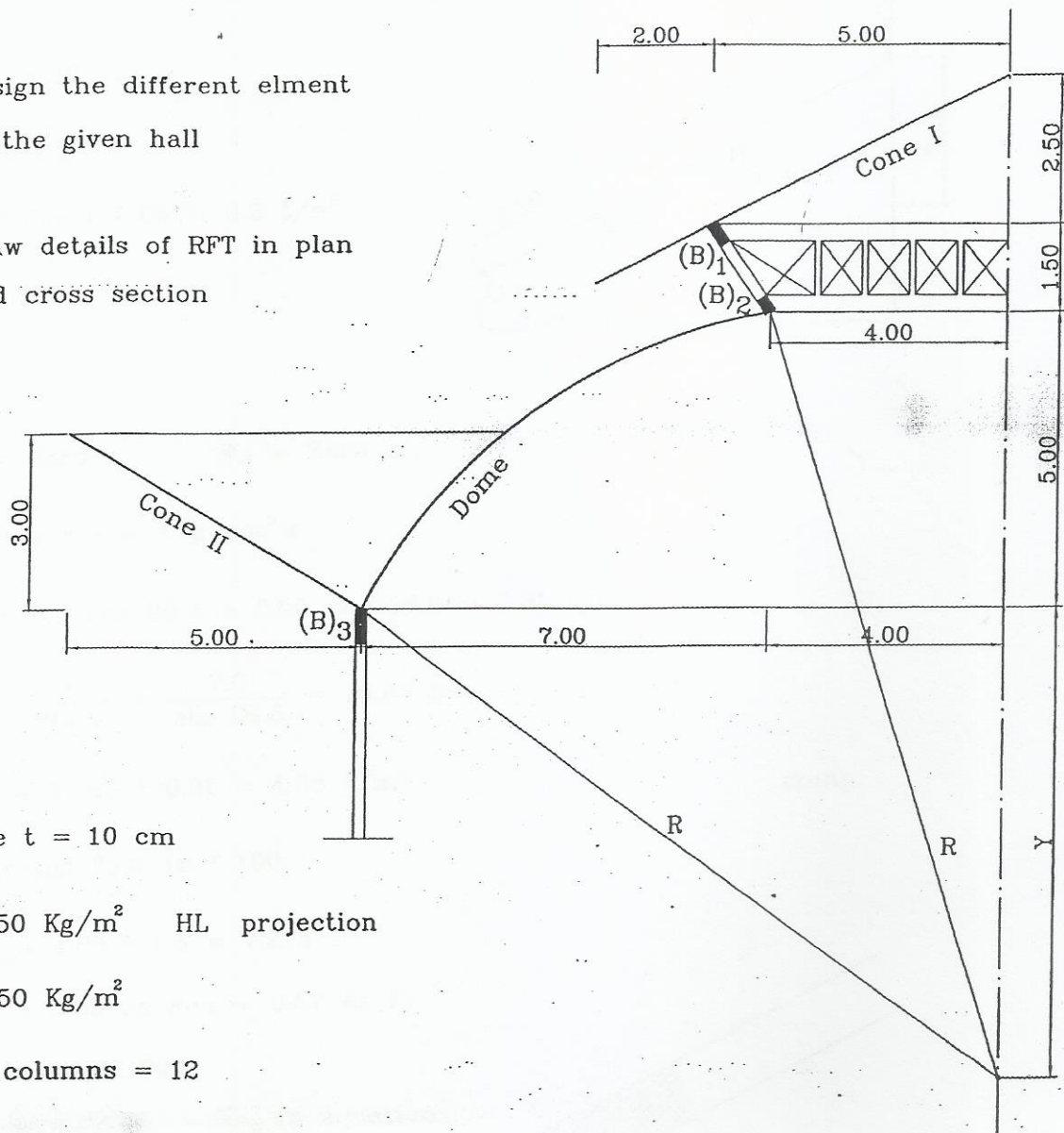




$$N.F = H \cdot r = 36 \cdot 3.57 = 128.52 \text{ t} \quad \text{comp.}$$

Example (7)

- Design the different element of the given hall
- Draw details of RFT in plan and cross section



assume $t = 10 \text{ cm}$

L.L = 50 Kg/m^2 HL projection

F.c = 50 Kg/m^2

no. of columns = 12

$$R^2 = (4)^2 + (5 + Y)^2$$

$$R^2 = (11)^2 + (Y)^2$$

$$16 + 25 + 10Y + Y^2 = 121 + Y^2$$

$$Y = 8.0 \text{ m}$$

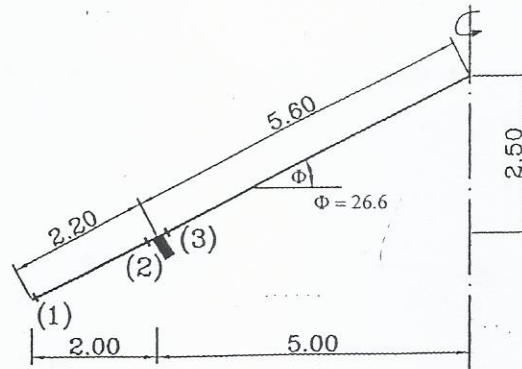
$$R = 13.6 \text{ m}$$

Cone I

assume $t = 10$ cm

$$g = o.w + F.c$$

$$g = 0.1 * 2.5 + 0.05 = 0.3 \text{ t/m}^2$$

Sec. (1)

$$T_1 = \text{Zero} \quad W_\phi = \text{Zero}$$

$$Z = g \cos \phi + p \cos^2 \phi$$

$$= 0.3 \cos 26.6 + 0.05 \cos^2 26.6 = 0.31 \text{ t/m}^2$$

$$R_2 = \frac{r}{\sin \phi} = \frac{7.0}{\sin 26.6} = 15.63 \text{ m}$$

$$T_2 = 15.63 * 0.31 = 4.85 \text{ t/m}^2$$

comp.

** sec resist $T_2 = 10 * 100$

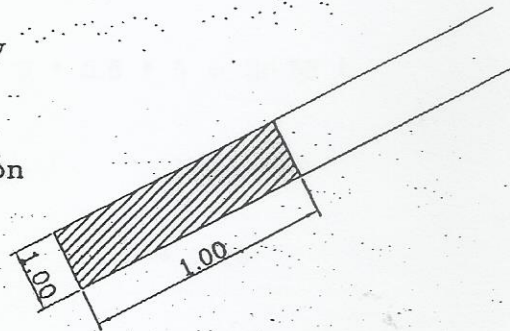
$$T_{2u} = 4.85 * 1.5 = 7.275 \text{ t}$$

$$P_u = 0.35 A_c F_{cu} + 0.67 A_s F_y$$

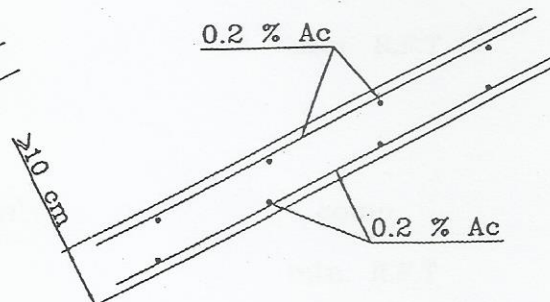
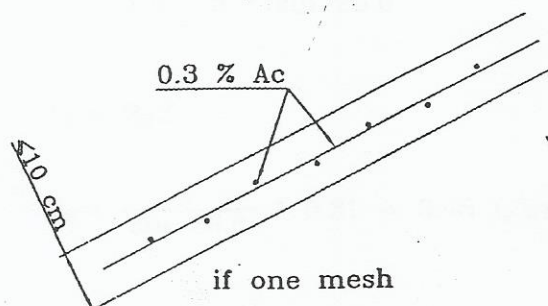
$$A_c = 10 * 100$$

take $P_u = 7.275 \text{ t} = T_{2u}$ in equation

$$A_s \text{ min} =$$



Min RFT for surface of revolution



Sec. (2)

$$W_{\Phi} = 0.05 * \pi * (7^2 - 5^2) + 0.3 * \pi * 2.2 * (5 + 7) = 11.69 \text{ t}$$

$$T_1 = \frac{W_{\Phi}}{2 \pi r \sin \phi}$$

$$r = 5.0$$

$$\phi = 26.6$$

$$T_1 = \frac{11.69}{2 \pi * 5 * \sin 26.6} = 4.16 \text{ t/m} \quad \text{ten.}$$

$$T_1 u = 4.16 * 1.5 = 6.24 \text{ t/m}$$

$$A_s = \frac{T_1 u}{F_y / \gamma_s} = \frac{6.24}{3.6 / 1.15} = 1.73 \text{ cm}^2 = 508 / \text{m}$$

$$T_2 = R_2 Z$$

$$T_2 = \frac{5}{\sin 26.6} * 0.31 = 3.46 \text{ t/m} \quad \text{comp.}$$

min. R.F.T

Sec. (3)

$$W_{\Phi} = 0.05 * \pi * (5^2) + 0.3 * \pi * 5.6 * 5 = 30.32 \text{ t}$$

$$T_1 = \frac{W_{\Phi}}{2 \pi r \sin \phi}$$

$$r = 5.0$$

$$\phi = 26.6$$

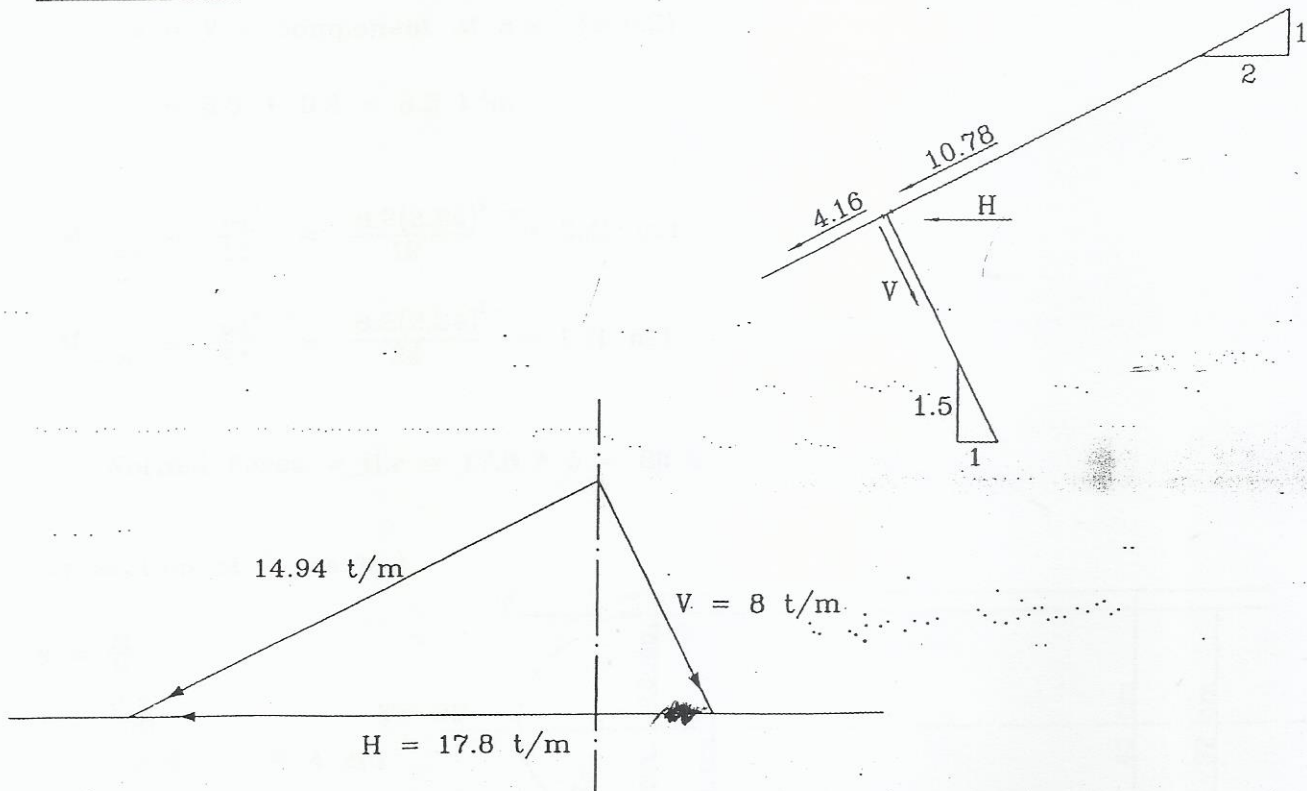
$$T_1 = \frac{30.32}{2 \pi * 5 * \sin 26.6} = 10.78 \text{ t/m} \quad \text{comp.}$$

min. R.F.T

$$T_2 = R_2 Z$$

$$T_2 = \frac{5}{\sin 26.6} * 0.31 = 3.46 \text{ t/m} \quad \text{comp.}$$

min. R.F.T

Design of B₁

assume sec. 20×40

$$o.w = 0.2 \times 0.4 \times 2.5 = 0.2 \text{ t/m}^2$$

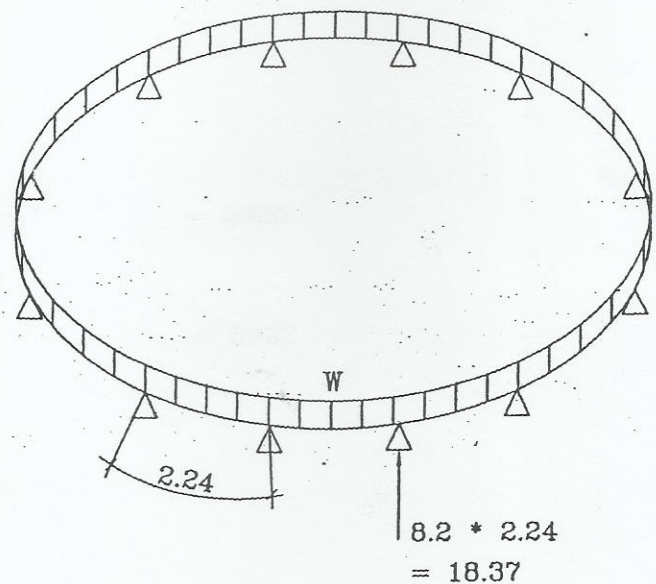
assume no. of posts = 14

no. of columns > 12

\therefore neglect torsion

$$M_{+ve} = \frac{wL^2}{12}$$

$$M_{-ve} = \frac{wL^2}{24}$$



$$w = V + \text{component of o.w } (\approx 0.2)$$

$$= 8.0 + 0.2 = 8.2 \text{ t/m}$$

$$M_{+ve} = \frac{wL^2}{12} = \frac{8.2(2.24)^2}{12} = 3.42 \text{ m.t}$$

$$M_{-ve} = \frac{wL^2}{24} = \frac{8.2(2.24)^2}{24} = 1.71 \text{ m.t}$$

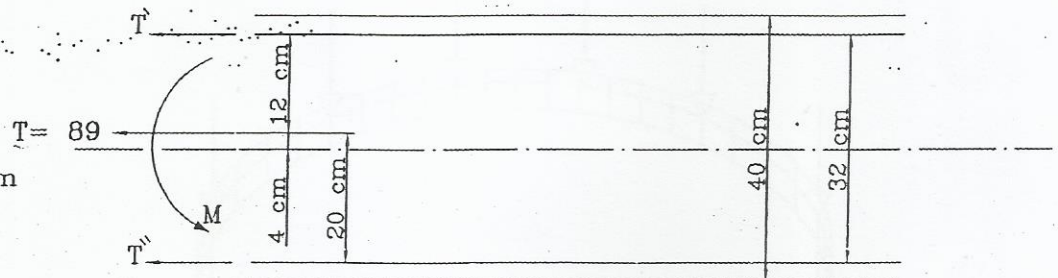
$$\text{Normal Force} = H.r = 17.8 * 5 = 89 \text{ t} \quad \text{ten.}$$

for section of (-ve M)

$$e = \frac{M}{N}$$

$$= \frac{3.42}{89}$$

$$= 0.384 \approx 4 \text{ cm}$$



$e < (\frac{t}{2} - \text{cover})$ small ecc. ten.

$$T' = 89 * \frac{20}{32} = 55.6 \text{ t}$$

$$T'' = 89 * \frac{12}{32} = 33.4 \text{ t}$$

$$As_1 = \frac{T'u}{F_y/\gamma_s} = \frac{55.6 * 1.5}{3.6/1.15} = 26.64 \text{ cm}^2 = 6\phi 25$$

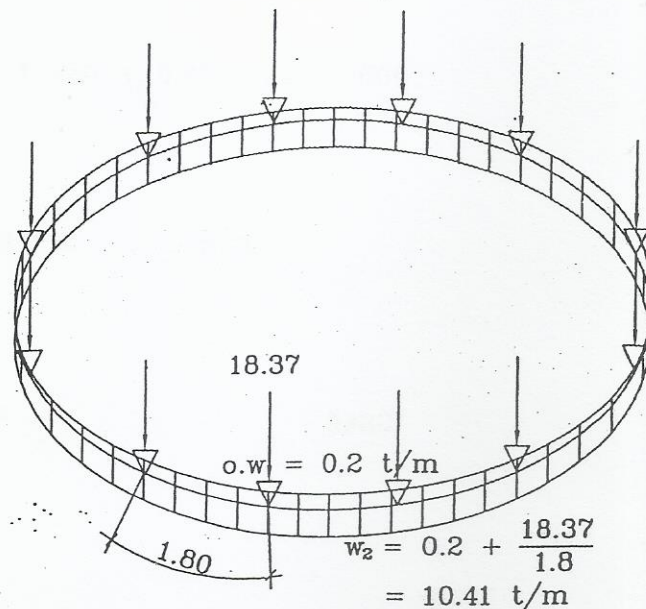
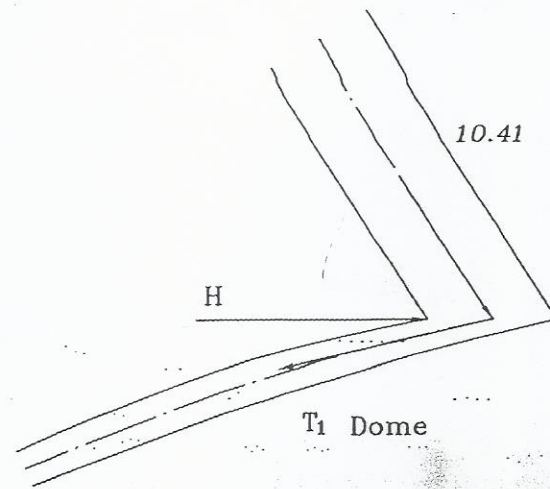
$$As_2 = \frac{T''u}{F_y/\gamma_s} = \frac{33.4 * 1.5}{3.6/1.15} = 16 \text{ cm}^2 = 5\phi 22$$

Post

$$P_u = 18.37 * 1.5$$

assume sec. 20 * 20

4\phi 12

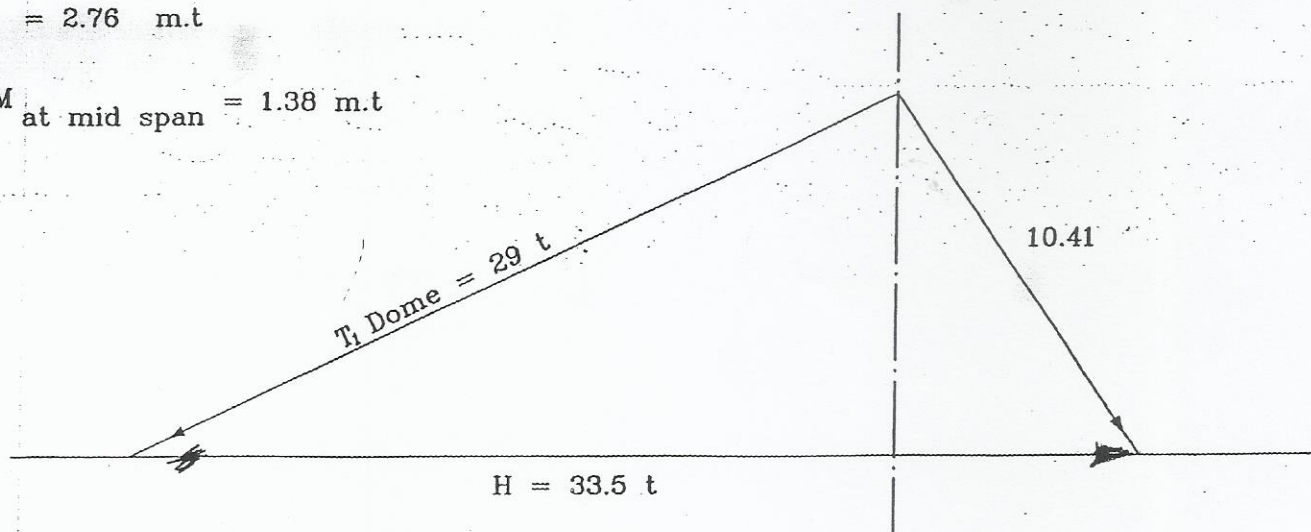
Design of B₂

$$M_{\text{at support}} = \frac{wL^2}{12}$$

$$= \frac{(10.41 - 0.2)^2 \cdot 1.8}{12}$$

$$= 2.76 \text{ m.t}$$

$$M_{\text{at mid span}} = 1.38 \text{ m.t}$$



$$N.F = 33.5 * 4 = 134 \text{ t}$$

comp.

$$e = \frac{M}{N} = \frac{2.76}{134} = 0.02 \text{ m}$$

$$\frac{e}{t} = \frac{0.02}{0.40} = 0.05$$

∴ neglect M

$$P_u = 0.35 A_c F_{cu} + 0.67 A_s F_y$$

$$A_c = 20 * 40$$

$$P_u = 134 * 1.5$$

$$134 * 1.5 * 10^3 = 0.35 * 20 * 40 * 250 + 0.67 * A_s * 3600$$

$$A_s = 54.3 \text{ cm}^2$$

$$\mu = \frac{A_s}{A_c} = \frac{54.3}{20 * 40} * 100 = 6.8 \% > 3 \%$$

take sec. 20 * 70

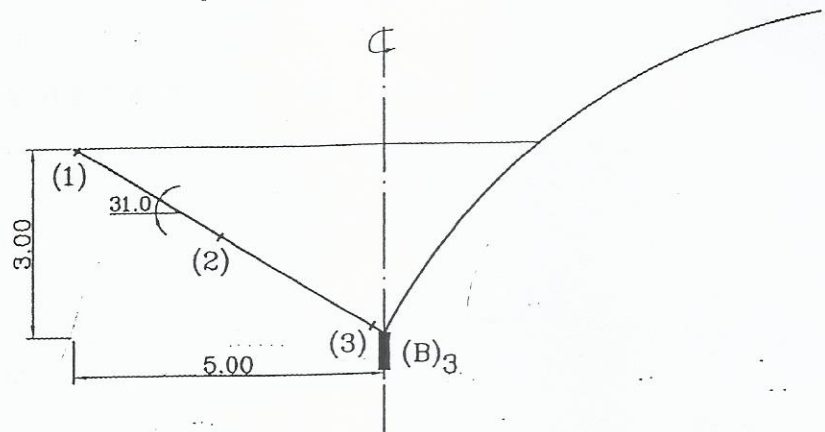
$$A_s = 32.54 \text{ cm}^2$$

9Ø22

$$\mu = 2.32 \%$$

Cone II

$$\begin{aligned}
 Z &= g \cos \phi + p \cos^2 \phi \\
 &= 0.3 \cos 31 + 0.05 \cos^2 31 \\
 &= 0.29 \text{ t/m}^2
 \end{aligned}$$

Sec. (1)

$$T_1 = \text{Zero}$$

$$W_\phi = \text{Zero}$$

$$T_2 = R_2 \cdot Z$$

$$R_2 = \frac{r}{\sin \phi} = \frac{16.0}{\sin 31.0} = 31.06 \text{ m}$$

$$T_2 = 31.06 \cdot 0.29 = 9.0 \text{ t/m}$$

Tension

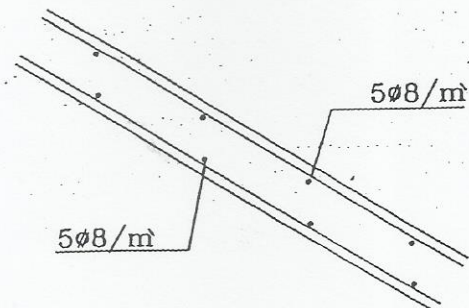
$$A_{s1} = \frac{T_u}{F_y/\gamma_s} = \frac{9.0 \cdot 1.5}{3.6/1.15} = 4.31 \text{ cm}^2 \quad \text{two sides}$$

$$A_{s/\text{side}} = 2.155 \text{ cm}^2 = 5\phi 8/\text{m} \text{ each side}$$

T_2 of sec. (2) & (3)

is not required since

A_{s1} of $T_{2 \max}$ (at sec.(1)) min. R.F.T



double mesh or
5\phi 8/m

Sec. (3)

$$W_{\Phi} = 0.5 * \pi * ((16)^2 - (11)^2) + 0.3 * \pi * 5.83 (16 + 11)$$

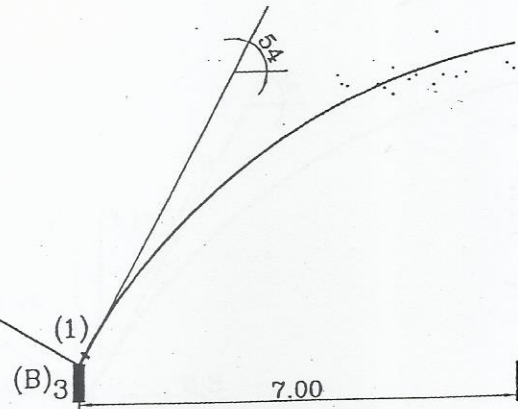
$$= 169.56 \text{ ton}$$

$$T_1 = \frac{W_{\Phi}}{2 \pi r \sin \Phi}$$

$$r = 11$$

$$\Phi = 31.0^\circ$$

$$T_1 = \frac{169.56}{2 \pi * 11 * \sin 31} = 4.76 \text{ t/m} \quad \text{comp.}$$

DomeSec. (1)

$$W_{\Phi} = 0.05 * \pi * 7^2 + 0.3 * \pi * 7.8 * 7.0$$

$$+ 0.2 * 2 * \pi * 5 + 0.2 * 0.2 * 0.5 * 2.5 * 14$$

$$+ 0.2 * 0.6 * 2.5 * 2 * \pi * 4 + 0.05 * \pi * (11 - 4)$$

$$+ 0.3 * 2 * \pi * 13.6 * 5 = 218.35 \text{ t}$$

$$T_1 = \frac{W_{\Phi}}{2 \pi r \sin \Phi}$$

$$r = 11$$

$$\Phi = 54$$

$$T_1 = \frac{218.35}{2 \pi * 11 * \sin 54} = 3.90 \text{ t/m} \quad \text{comp.}$$

$$Z = g \cos \phi + p \cos^2 \phi$$

$$= 0.05 \cos 54 + 0.3 \cos 54 = 0.19 \text{ t/m}^2$$

$$T_1 + T_2 = R Z$$

$$T_2 = 13.6 * 0.19 - 3.9$$

$$= -1.32 \text{ t/m}^2 \quad \text{ten.}$$

min. R.F.T

508/m

Design of B3

assume no. of column

$$= 10$$

assume sec. 35 * 80

$$w = 3.16 + 2.45 + \text{component of o.w}$$

$$= 3.16 * 2.45 + 0.35 * 0.85 * 2.5$$

$$= 6.31 \text{ t/m}^2$$

$$P = w * 2 \pi * r$$

$$= 6.31 * 2 * \pi * 11$$

$$= 436.12 \text{ t}$$

$$\text{Load / col.} = \frac{P}{10} = 43.61 \text{ ton}$$

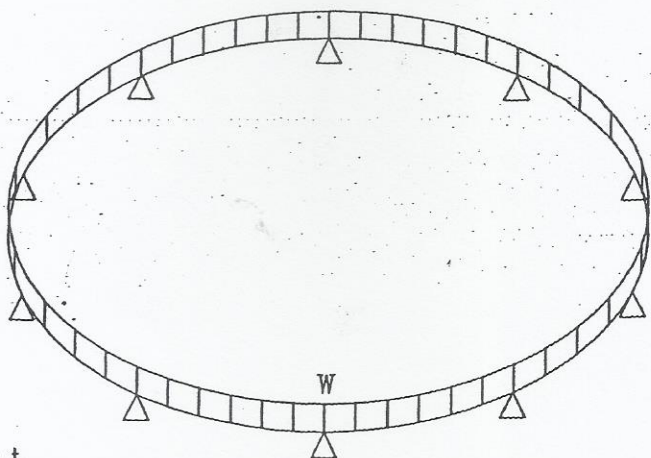
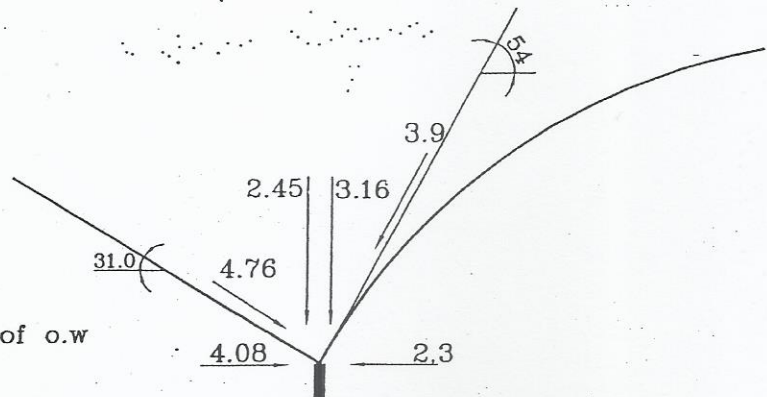
$$Q_{\max.} = \frac{P}{2*10} = 21.8 \text{ ton}$$

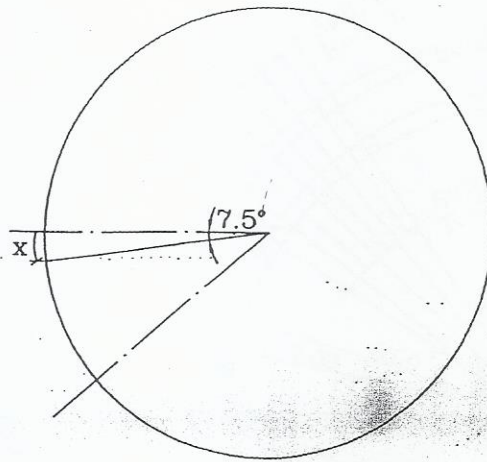
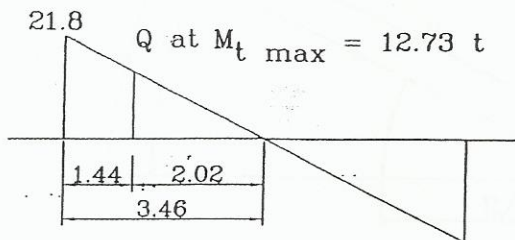
$$N = (4.08 - 2.3) * 11 = 19.58 \text{ t comp.}$$

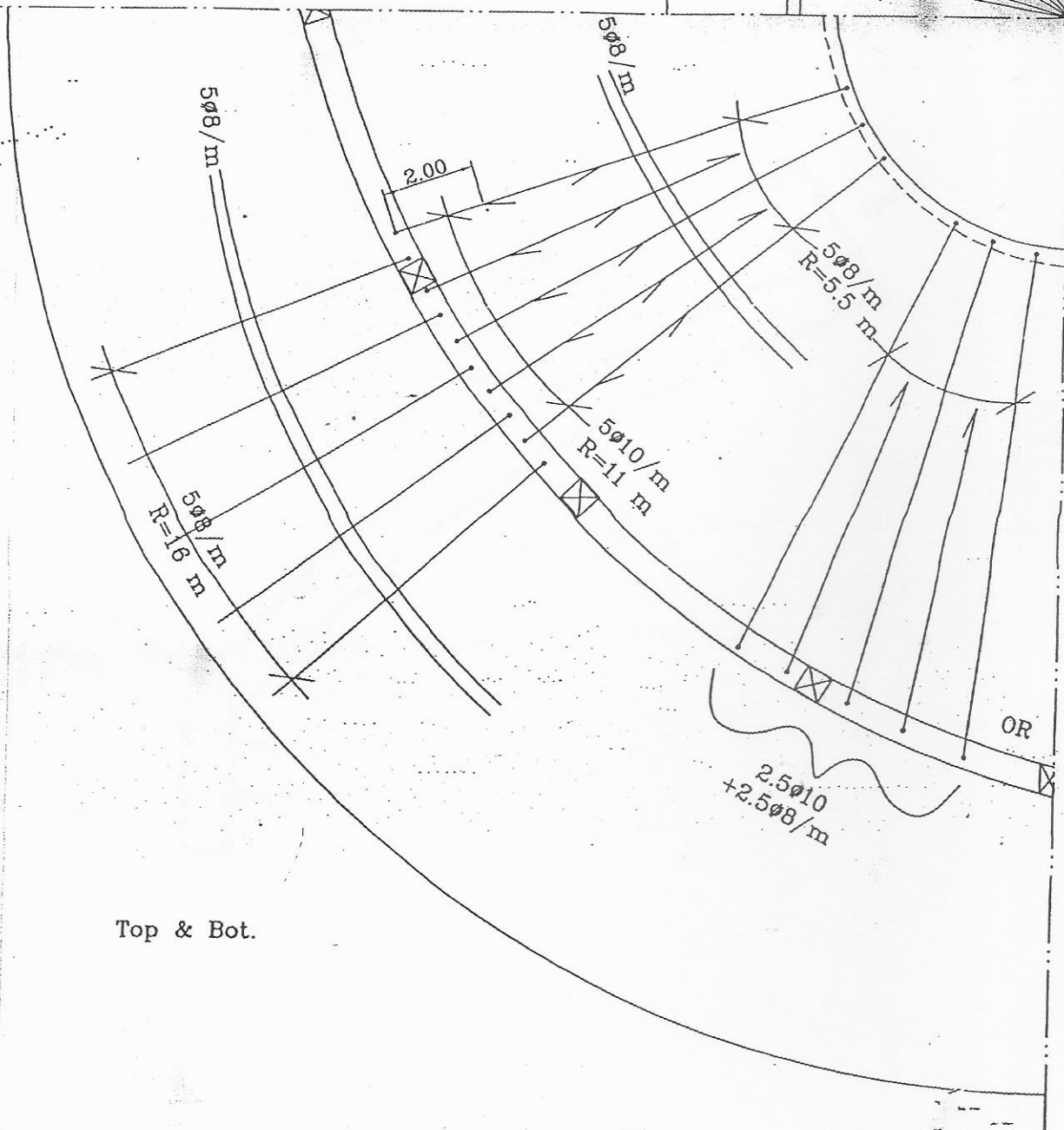
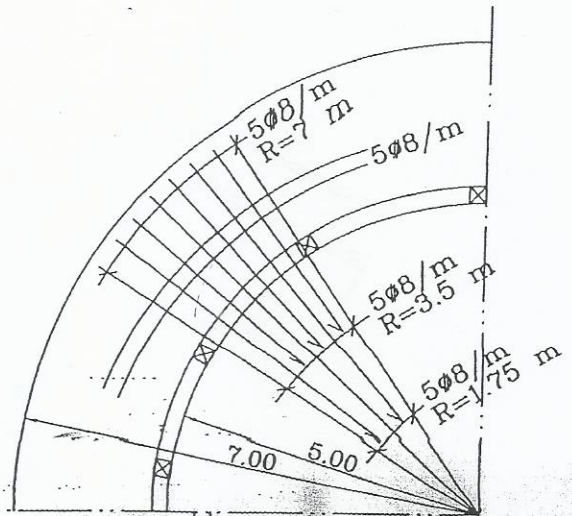
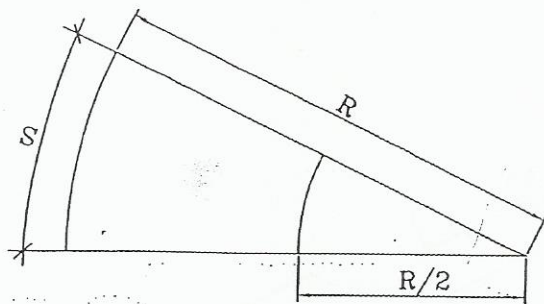
$$M_{+ve} = 0.0032 * 436.12 * 11 = 15.35 \text{ m.t}$$

$$M_{-ve} = 0.0052 * 436.12 * 11 = 24.95 \text{ m.t}$$

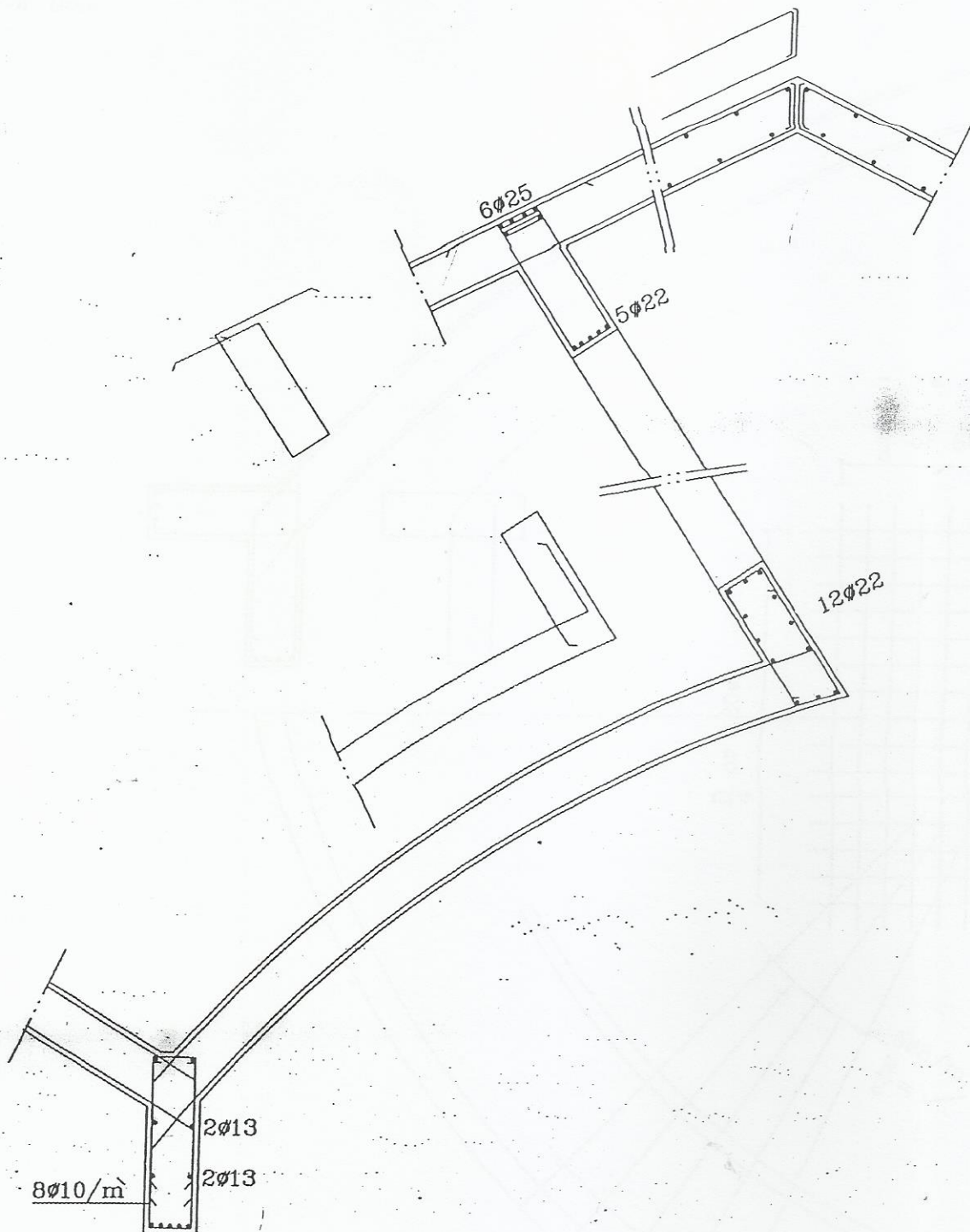
$$M_t = 0.0004 * 436.12 * 11 = 1.92 \text{ m.t}$$



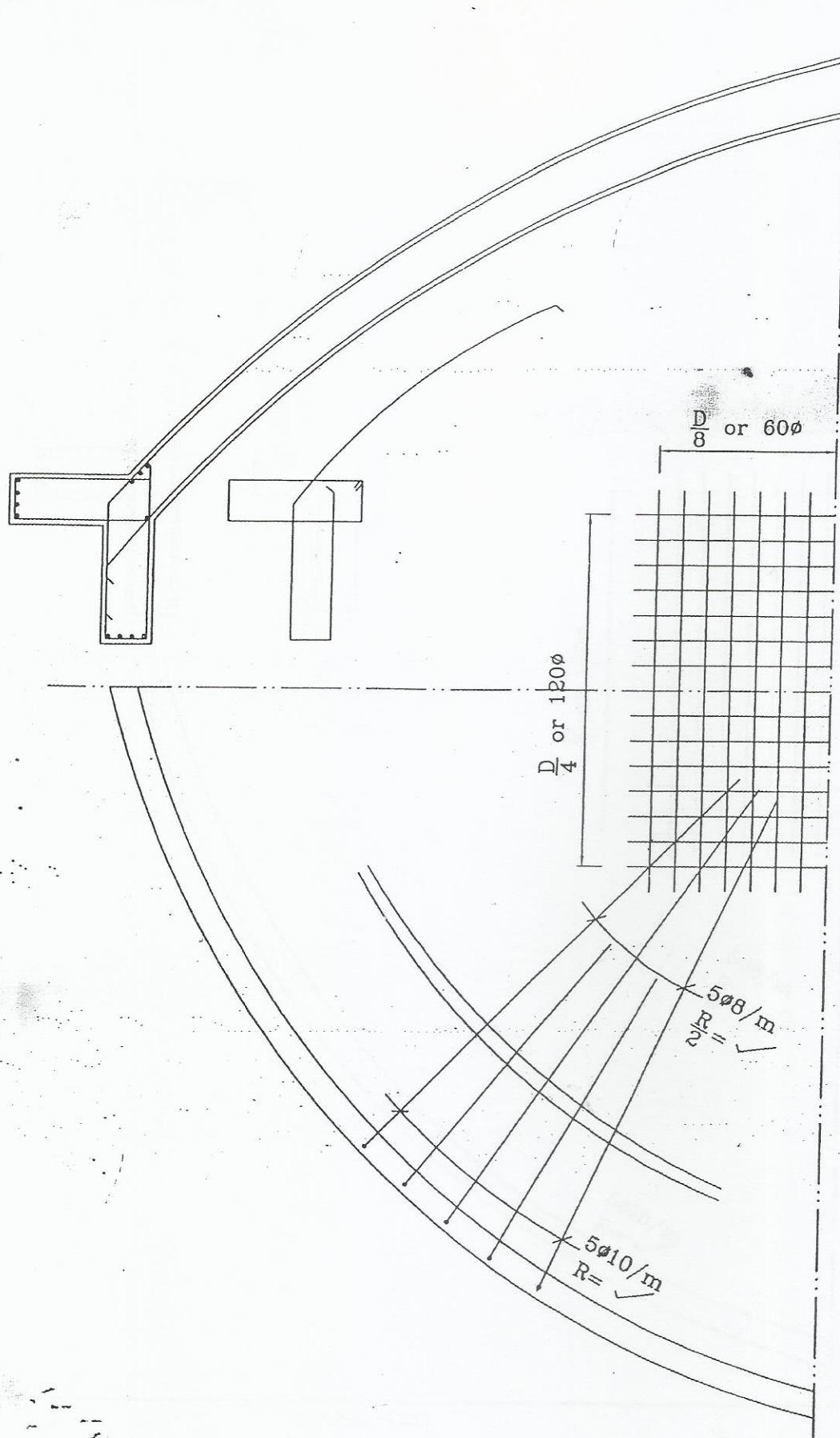


Details of R.F.T

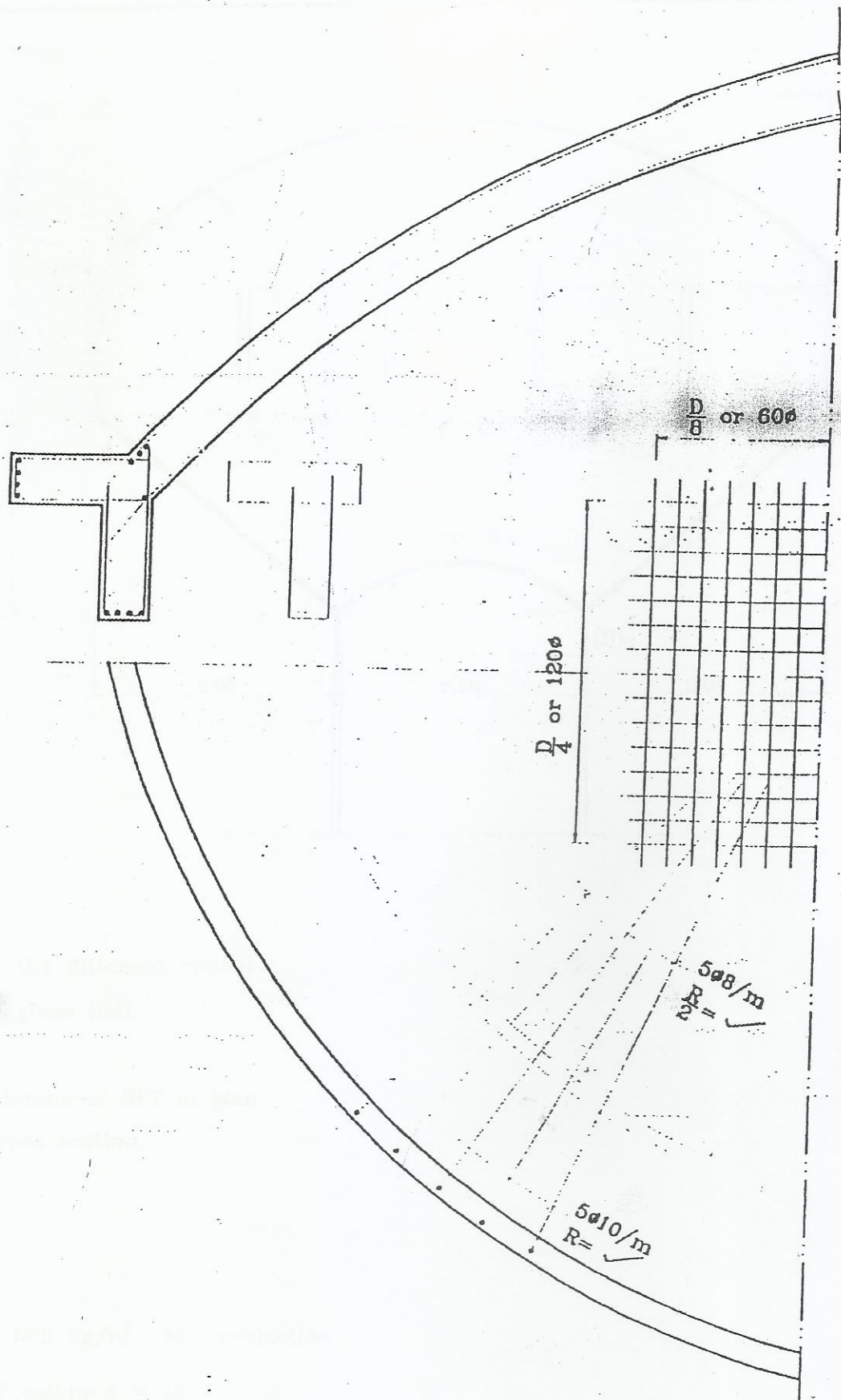
Top & Bot.

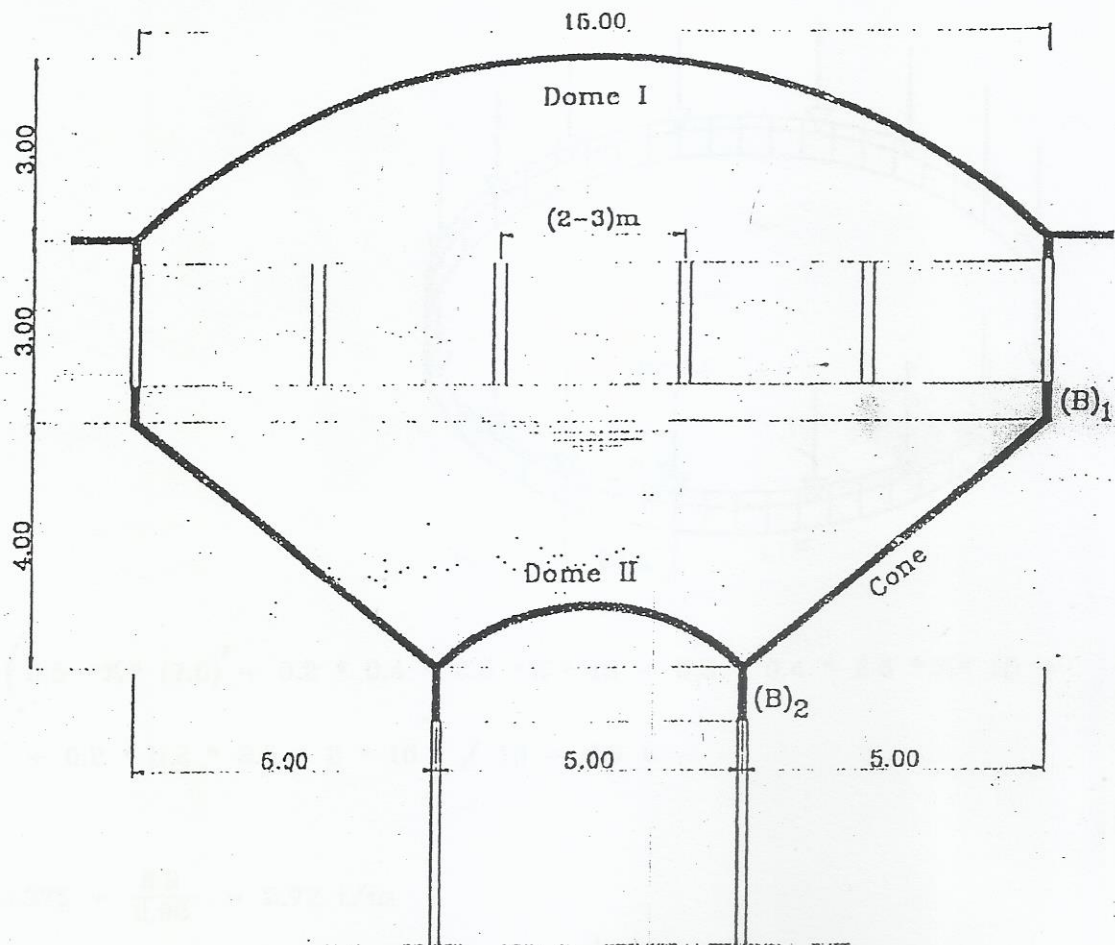


For Dome



For Dome



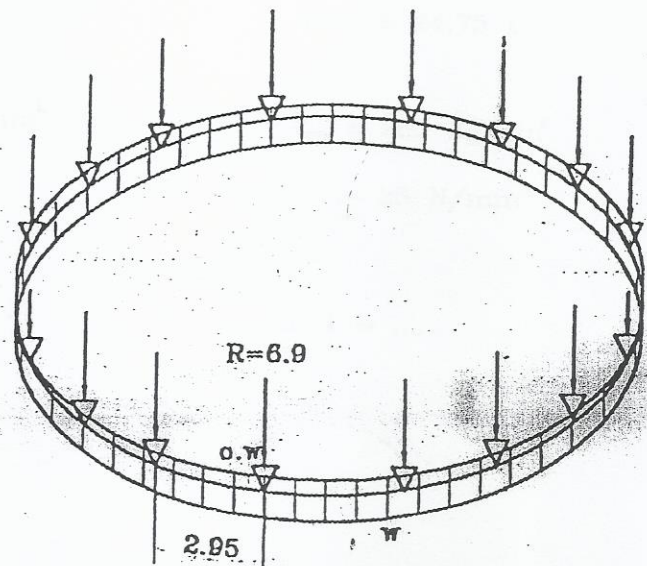
Example (8)

- Design the different element of the given hall
- Draw details of RFT in plan and cross section

assume

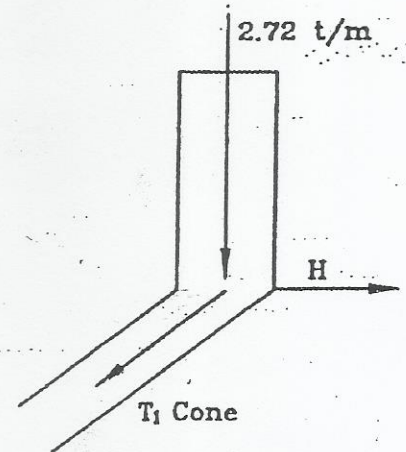
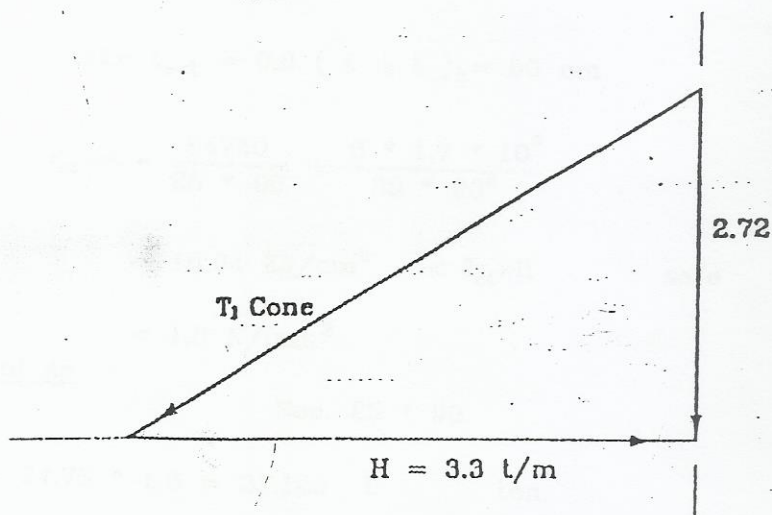
T.L = 500 Kg/m² HL projection

no. of columns = 16

Design of B₁

$$R = \left(0.6 \cdot \pi \cdot (7.6)^2 + 0.2 \cdot 0.4 \cdot 2.5 \cdot \pi \cdot 15 + 0.2 \cdot 0.4 \cdot 2.5 \cdot \pi \cdot 15 + \right. \\ \left. + 0.2 \cdot 0.2 \cdot 2.5 \cdot 2 \cdot 10 \right) / 16 = 6.9 \text{ t}$$

$$w = 0.375 + \frac{6.9}{2.95} = 2.72 \text{ t/m}$$



$$N.F = H \cdot r$$

$$= 3.3 \cdot 7.5 = 24.75 \text{ t}$$

ten.

$$M_1 = \frac{W_{nat}(L)^2}{12} = \frac{(2.72 - 0.375) \cdot (2.95)^2}{12} = 1.7 \text{ m.t}$$

Sec. of Beam B_g

$$M = 1.7 \text{ m.t}$$

$$N = + 24.75 \text{ t}$$

$$F_{ct \text{ all}} = 17 \text{ Kg/cm}^2 = 1.7 \text{ N/mm}^2$$

$$F_{cu} = 250 \text{ Kg/cm}^2$$

$$= 25 \text{ N/mm}^2$$

$$F_{ct \text{ all}} = \frac{N}{A} + \frac{M}{Z}$$

$$= \frac{N}{b.t} + \frac{6 M}{b.t^2}$$

$$\therefore t = \dots$$

or neglect M

$$F_{ct \text{ all}} = \frac{N}{A} = \frac{N}{b.t}$$

$$17 = \frac{24750}{25 * t_1}$$

$$\therefore t_1 = 58 \text{ cm}$$

neglect N

$$F_{ct \text{ all}} = \frac{M}{Z} = \frac{6 M}{b.t^2}$$

$$17 = \frac{6 * 1.7 * 10^5}{25 * (t_2)^2}$$

$$\therefore t_2 = 50 \text{ cm}$$

$$\text{take } t_{act} = 0.8 (t_1 + t_2) = 90 \text{ cm.}$$

$$F_{ct \text{ act}} = \frac{24750}{25 * 90} + \frac{6 * 1.7 * 10^5}{25 * 90^2}$$

$$= 16.04 \text{ Kg/cm}^2 < F_{ct \text{ all}}$$

safe

$$= 1.6 \text{ N/mm}^2$$

Cal. of A_s

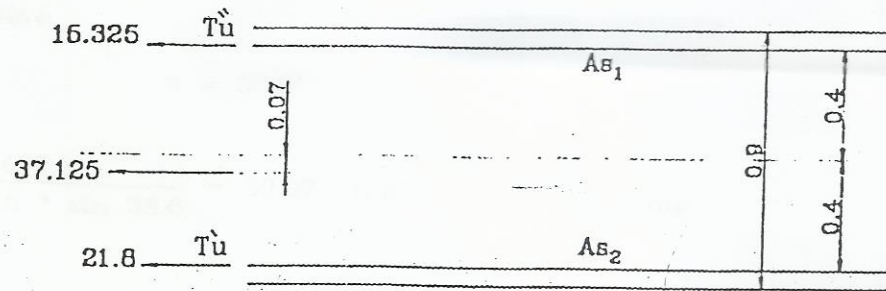
Sec. 25 * 90

$$N_u = 24.75 * 1.5 = 37.125 \text{ t} \quad \text{ten.}$$

$$M_u = 1.7 * 1.5 = 2.55 \text{ m.t}$$

$$e = \frac{M}{N} = \frac{2.55}{37.125} = 0.07 < \frac{t}{2} - \text{cover}$$

Small ecc. Ten.



$$B = 0.75 \quad \text{H.T.S.} \quad (13, 16)$$

$$As_1 = \frac{T_u}{F_y/\gamma_s} = \frac{21.8}{0.75(3.6/1.15)} = 9.50 \text{ cm}^2 = 5\phi 16$$

$$As_2 = \frac{T_u}{F_y/\gamma_s} = \frac{15.325}{0.75(3.6/1.15)} = 6.53 \text{ cm}^2 = 4\phi 16$$

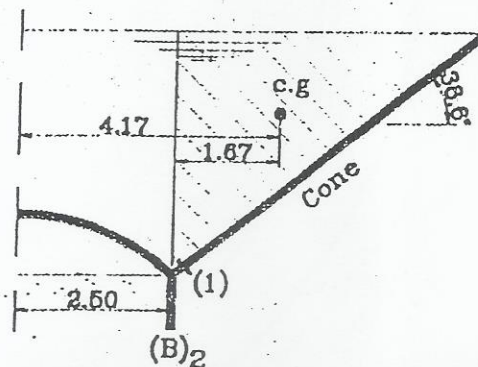
Cone

assume $t_s = 20 \text{ cm}$

$$g = 0.6 \text{ t/m}^2$$

Sec. (1)

$$\begin{aligned} W_\phi &= 0.5 \cdot \pi \cdot (7.5)^2 \\ &+ 0.2 \cdot 0.4 \cdot 2.5 \cdot 2 \cdot \pi \cdot 15 \\ &+ 0.2 \cdot 0.2 \cdot 2.5 \cdot 2 \cdot \pi \cdot 16 \\ &+ 0.25 \cdot 0.9 \cdot 2.5 \cdot \pi \cdot 15 \\ &+ 0.5 \cdot \pi \cdot 6.4 \cdot (7.5 + 2.5) \\ &+ 1/2 \cdot 4 \cdot 5 \cdot 2 \cdot \pi \cdot 4.77 \\ &= 499.2 \text{ ton} \end{aligned}$$



Dome

hL & vL

Posts

B₂

o.w

Water

$$T_1 = \frac{W \phi}{2 \pi r \sin \phi}$$

$$r = 2.5$$

$$\phi = 38.6^\circ$$

$$T_1 = \frac{499.2}{2 \pi \cdot 2.5 \cdot \sin 38.6} = 50.97 \text{ t/m}^2$$

comp.

$$T_2 = R_2 Z$$

$$R_2 = \frac{r}{\sin \phi} = \frac{2.5}{\sin 38.6} = 4.0 \text{ m}$$

$$Z = g \cos \phi + \gamma h$$

$$= 0.5 \cos 38.6 + 1 \cdot 4 = 4.39 \text{ t/m}^3$$

$$T_2 = 4 \cdot 4.39 = 17.6 \text{ t/m}^2$$

ten.

** Design of Sec.

$$\text{Due to } T = 17.6 \text{ t}$$

$$\text{Sec.} = t \cdot 100$$

$$t = K \cdot T$$

$$= 0.59 \cdot 17.6 = 10.384 \text{ cm} < 20 \text{ cm}$$

safe

$$A_s = \frac{T_u}{B_{cr} (F_y / \gamma_s)} = \frac{17.6 \cdot 1.5}{0.75 \cdot \left(\frac{3.6}{1.15} \right)} = 11.24 \text{ cm}^2$$

5\phi 12

each side

Details of R.F.T

Dome (1)

