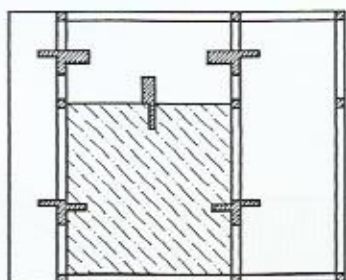


Mid Term Revision.

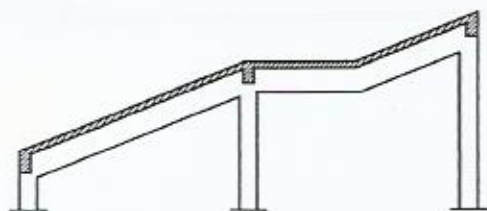
Important Examples.

①



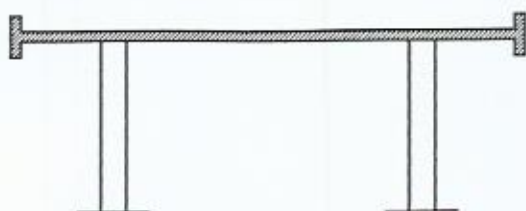
Solid Slabs EX. في ملزمه
Page 43

②

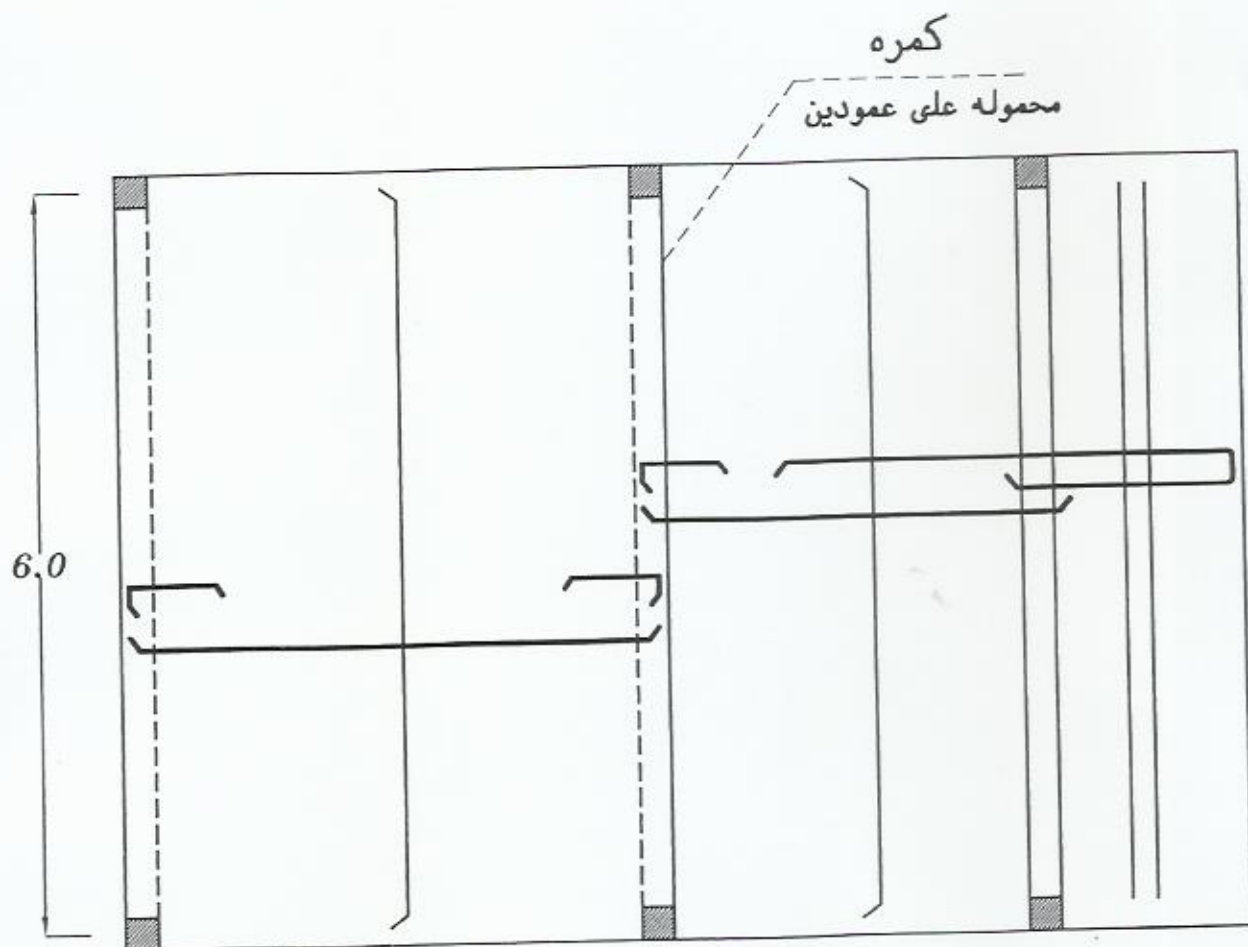
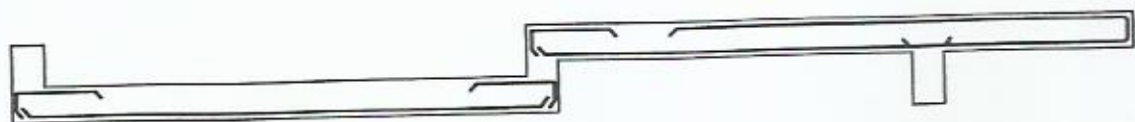
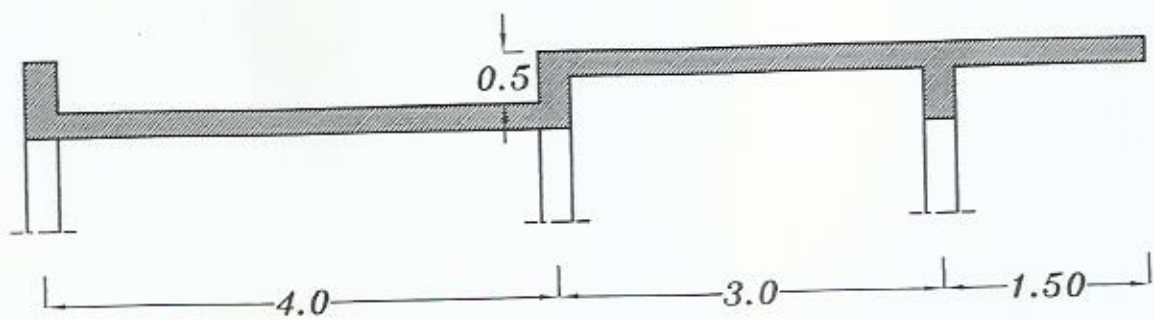


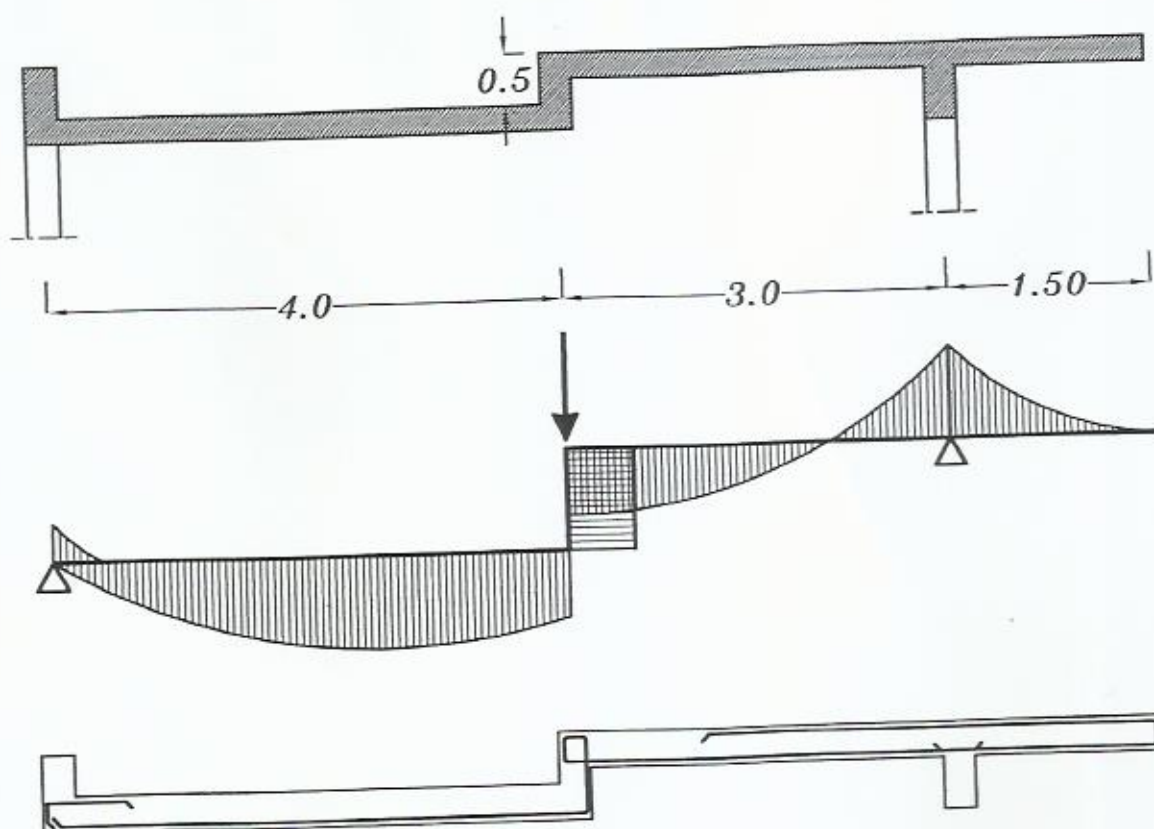
Solid Slabs EX. في ملزمه
Page 70

③

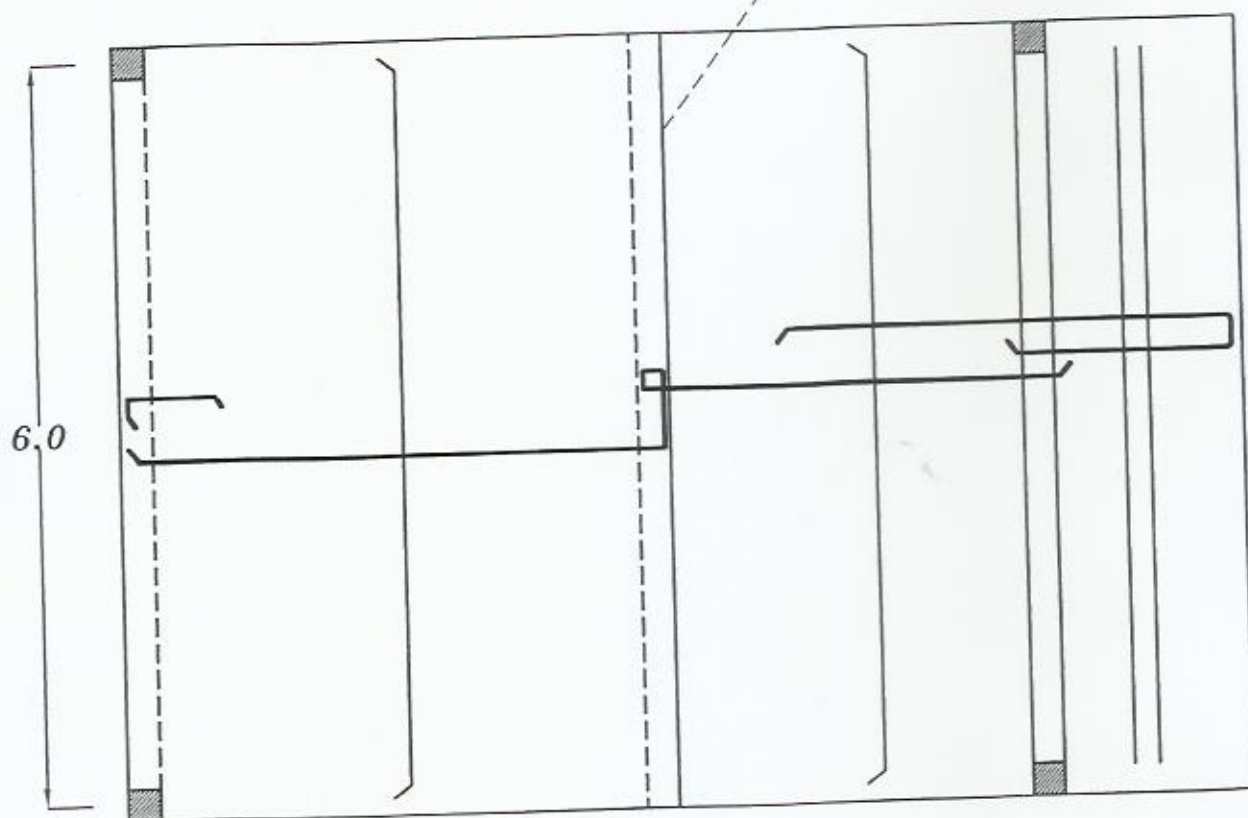


Flat Slabs EX. في ملزمه
Page 44





جزء من البلاطة
ليست محمولة على اعمده

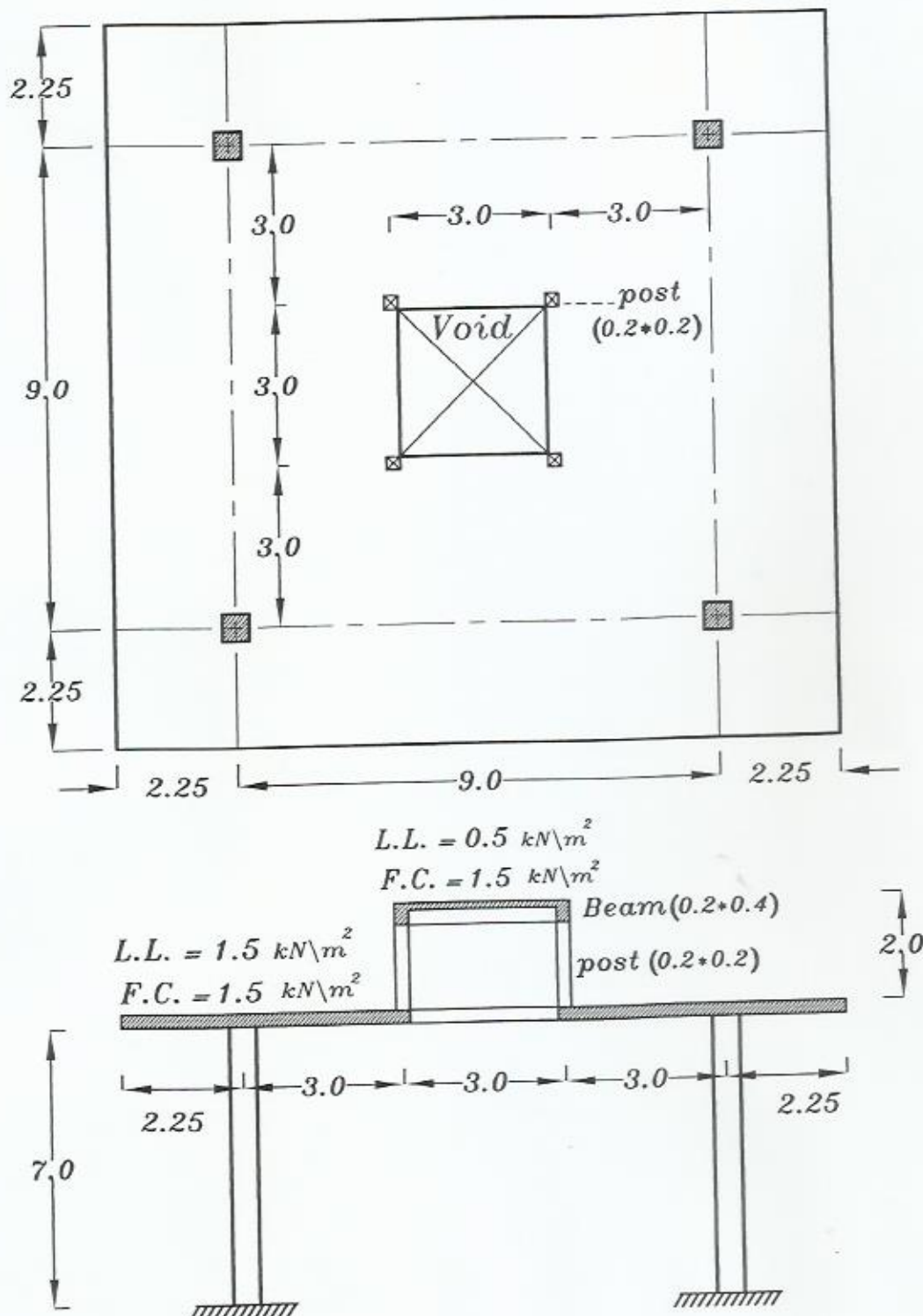


Example.

Data. $F_{cu} = 30 \text{ N/mm}^2$, $F_y = 360 \text{ N/mm}^2$

Req.

- ① Check punching shear of the slab at one of the columns.
- ② Using Frame analysis method, Design the slab assuming constant inertia and uniform load distribution (Case of total load only is required).
- ③ Draw a half plan showing details of reinforcement in both directions.



Solution.

1-Concrete Dimensions.

Column dimensions.

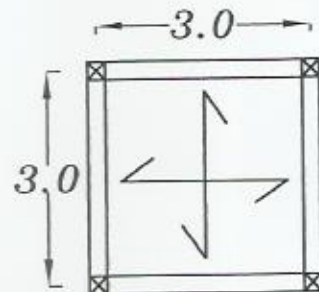
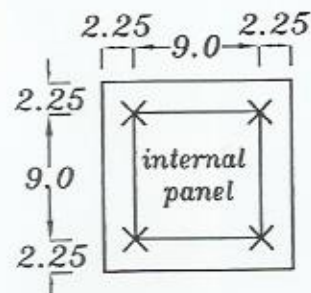
$$b_{col} = \begin{cases} 300 \text{ mm} \\ \frac{H}{15} = \frac{7000}{15} = 466.6 \text{ mm} \\ \frac{L_1}{20} = \frac{9000}{20} = 450 \text{ mm} \end{cases} \quad \boxed{b_{col} = 500 \text{ mm}} \\ (500 * 500)$$

Slab Thickness.

Flat Slab.

$$L_1 = 9.0 \text{ m}$$

$$\begin{array}{l} \text{Internal panel } t_s = \frac{L_1}{36} = \frac{9000}{36} = 250 \text{ mm} \\ \text{Cantilever } t_s = \frac{L_c}{10} = \frac{2250}{10} = 225 \text{ mm} \end{array} \quad \boxed{t_s = 250 \text{ mm}}$$



Solid slab. Two way

$$t_s = \frac{L_s}{35} = \frac{3000}{35} = 85.7 \text{ mm} \quad \boxed{t_s = 100 \text{ mm}}$$

2-Loads on the Slab.

Flat Slab.

$$w_s = 1.4 (t_s \delta_c + F.C.) + 1.6 (L.L.)$$

$$w_s = 1.4 (0.25 * 25 + 1.50) + 1.6 (1.50) = 13.25 \text{ kN/m}^2$$

Solid Slab.

$$w_s = 1.4 (0.10 * 25 + 1.50) + 1.6 (0.50) = 6.40 \text{ kN/m}^2$$

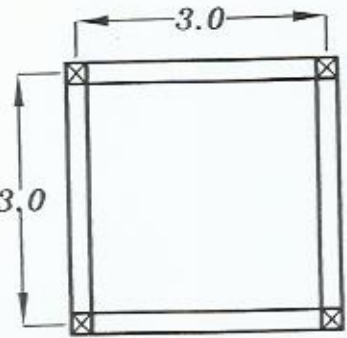
Loads on the Post.

Beam (200*400)

$$o.w. (beam) = 1.4 * 0.2 * 0.4 * 25 = 2.8 \text{ kN/m}$$

Post (200*200)

$$o.w. (Post) = 1.4 * 0.2 * 0.2 * 2.0 * 25 = 2.8 \text{ kN}$$



لتحديد الحمل على ال post الواحد

نحسب الوزن الكلي للشخشيخه من بلاطه و كمرات و posts
و نقسم الوزن الكلي على ٤ .

$$\text{Total Weight} = \text{Slab} + 4 \text{ Beams} + 4 \text{ Posts}$$

$$\text{Slab} = w_s * \text{area} = 6.40 * (3.0 * 3.0) = 57.6 \text{ kN}$$

$$4 \text{ Beams} = o.w. (beam) * \text{طول الكمرات} = 2.8 (3.0 * 4.0) = 33.6 \text{ kN}$$

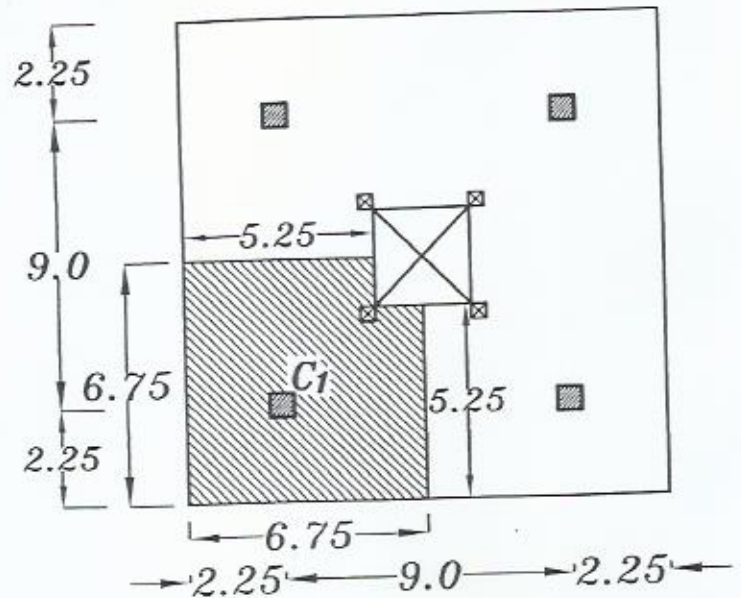
$$4 \text{ Posts} = 4 * 2.8 = 11.2 \text{ kN}$$

$$\text{Total Weight} = 57.6 + 33.6 + 11.2 = 102.4 \text{ kN}$$

$$\text{Load on One Post} = \frac{\text{Total Weight}}{4} = \frac{102.4}{4} = 25.6 \text{ kN}$$

Check Punching on interior column C₁

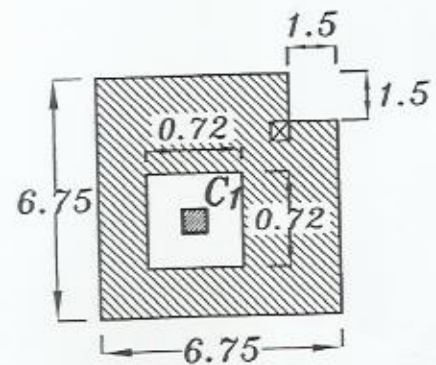
C₁ Interior Column.



$$d = t_s - 30 \text{ mm}$$

$$= 250 - 30 = 220 \text{ mm} = 0.22 \text{ m}$$

$$C+d = 0.50 + 0.22 = 0.72 \text{ m}$$



$$Q_{pu} = w_s [L_1 * L_2 - \text{void} - (C_1+d)(C_2+d)] + \text{Post}$$

$$Q_{pu} = 13.25 [6.75 * 6.75 - (1.5 * 1.5) - (0.72 * 0.72)] + 25.6$$

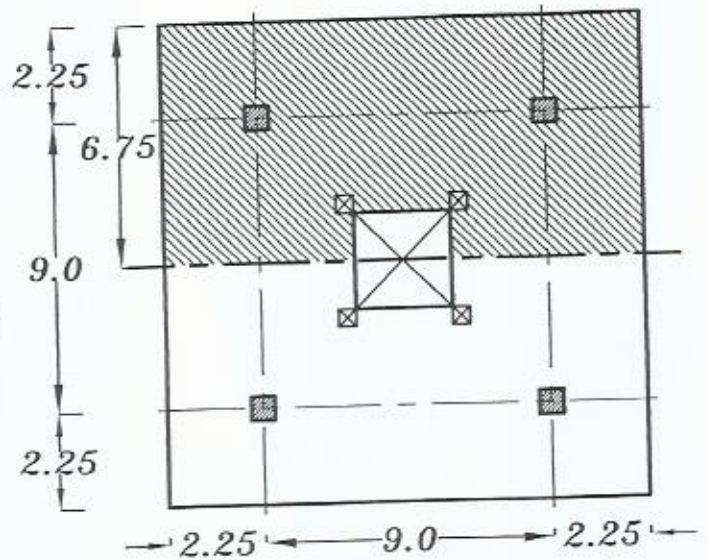
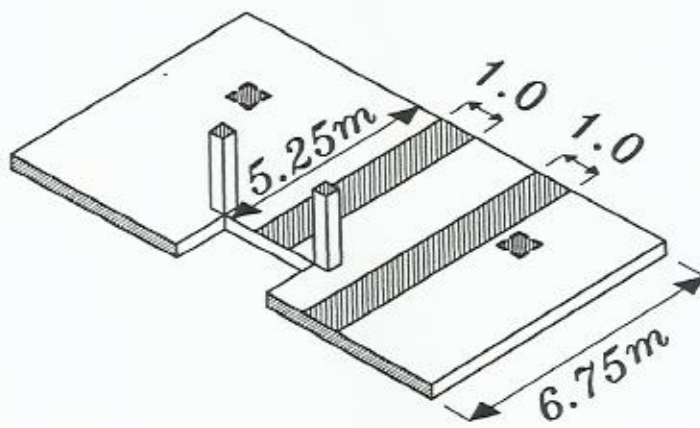
$$= 592.6 \text{ kN}$$

$$A_p = (b_o * d) = (4 * 720) * 220 = 633600 \text{ mm}^2$$

$$q_{pu} = \frac{Q_{pu}}{A_p} * \beta = \frac{592.6 * 10^3}{633600} * 1.15 = 1.07 \text{ N/mm}^2$$

$$q_{pcu} = 0.316 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.316 \sqrt{\frac{30}{1.5}} = 1.41 \text{ N/mm}^2$$

$$\boxed{q_{pu} < q_{pcu}} \rightarrow \text{Safe Punching.}$$



$$w_1 = w_s * L_2 = 13.25 * 6.75 = 89.43 \text{ kN/m}$$

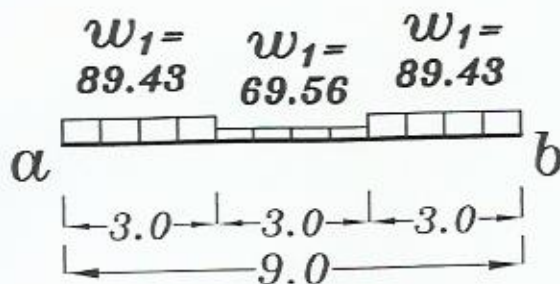
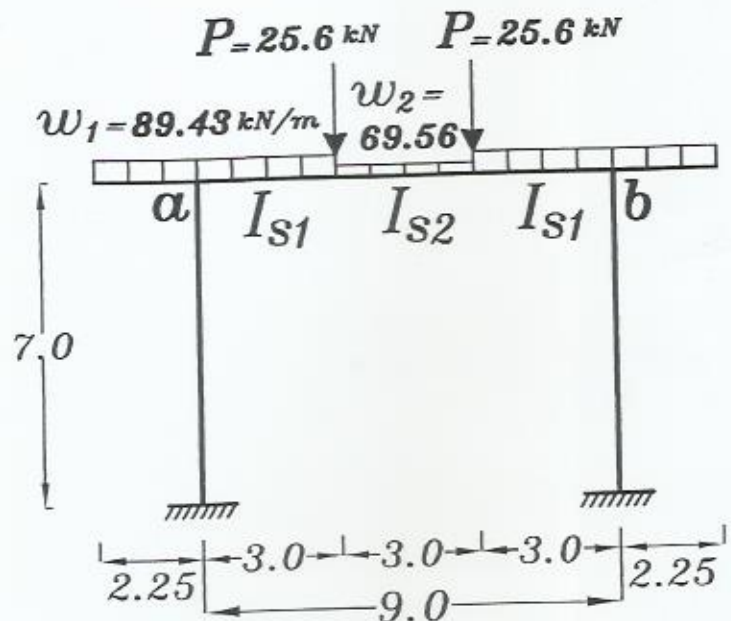
$$w_2 = w_s * L_2 = 13.25 * 5.25 = 69.56 \text{ kN/m}$$

للحل بطريقة

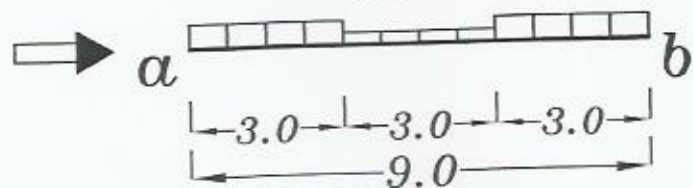
moment distribution

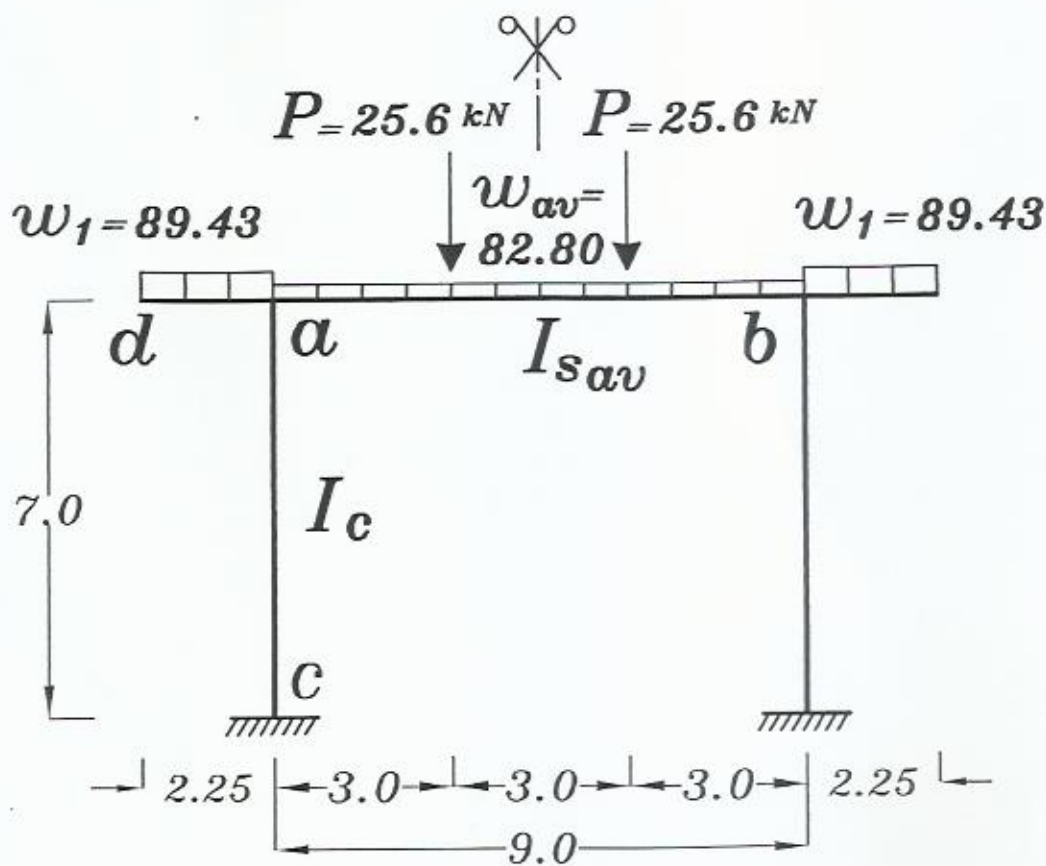
يجب أن يكون كل member

عليه حمل منتظم واحد



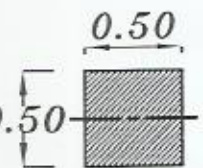
$$w_{av} = \frac{89.43 * 6.0 + 69.56 * 3.0}{9.0} = 82.80$$

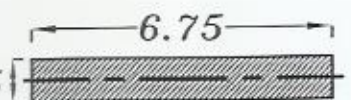




@ Calculate Moment of Inertia For Slabs & Columns.

عمود خارجی

$$I_c = 0.6 * \frac{b(t)^3}{12} = 0.6 * \frac{0.50 * 0.50^3}{12} = 3.125 * 10^{-3} m^4$$


$$I_{s1} = \frac{L_2 * t_s^3}{12} = \frac{6.75 * 0.25^3}{12} = 8.79 * 10^{-3} m^4$$


$$I_{s2} = \frac{L_2 * t_s^3}{12} = \frac{5.25 * 0.25^3}{12} = 6.83 * 10^{-3} m^4$$


$$I_{sav} = \frac{8.79 * 10^{-3} (6.0) + 6.83 * 10^{-3} (3.0)}{9.0} = 8.13 * 10^{-3} m^4$$

⑥ Calculate the stiffness For each member.

$$K_{ab} = \frac{1}{2} * \frac{I_{sav}}{L} = \frac{1}{2} * \frac{8.13 * 10^{-3}}{9.0} = 4.516 * 10^{-4}$$

$$K_{ac} = \frac{I_c}{h} = \frac{3.125 * 10^{-3}}{7.0} = 4.46 * 10^{-4}$$

⑦ Calculate the Distribution Factors. (D.F.)

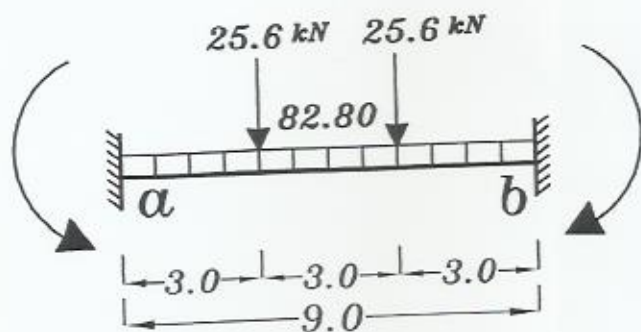
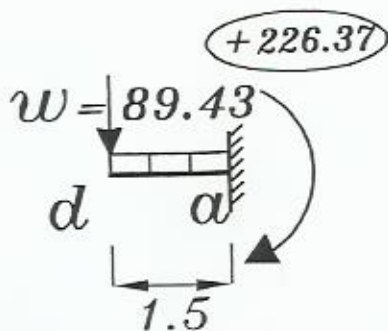
For Joint A

$$\Sigma K = K_{ab} + K_{ac} = 4.516 * 10^{-4} + 4.46 * 10^{-4} = 8.976 * 10^{-4}$$

$$D.F.(ab) = \frac{4.516 * 10^{-4}}{8.976 * 10^{-4}} = 0.503$$

$$D.F.(ac) = \frac{4.46 * 10^{-4}}{8.976 * 10^{-4}} = 0.497$$

⑧ Calculate Fixed End Moment For the Slab.

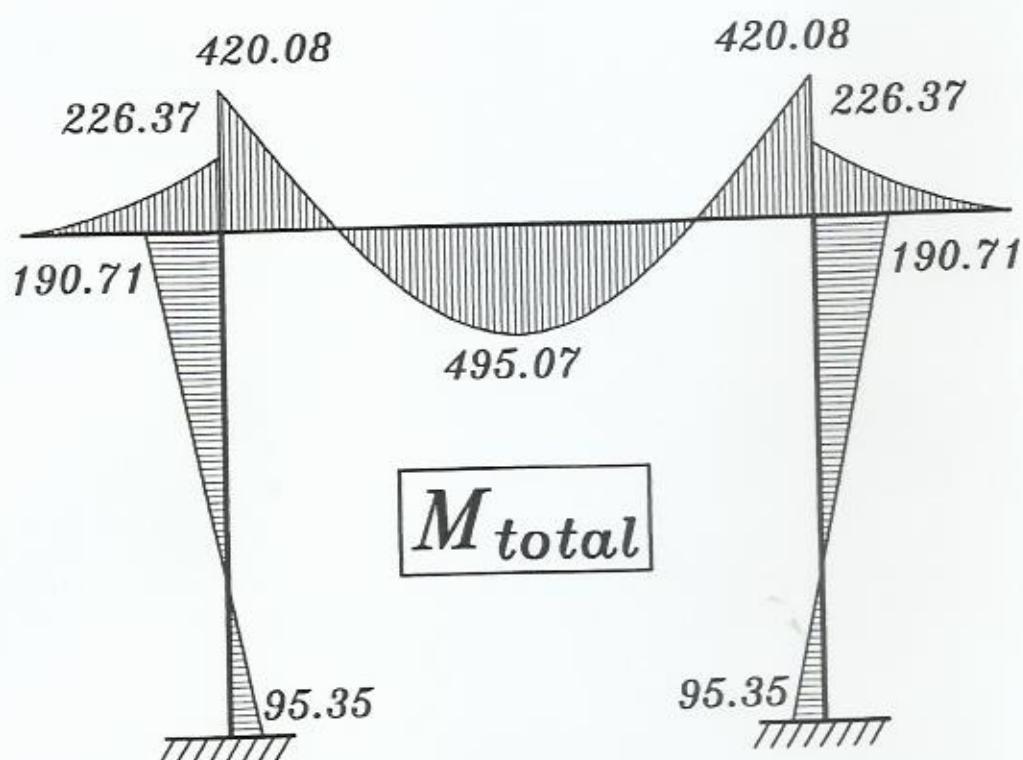


$$F.E.M.(ab) = -\frac{wL^2}{12} - \frac{2}{9} PL = -\frac{82.80 * 9.0^2}{12} - \frac{2}{9} (25.6)(9.0) = -610.1 \text{ kN.m.}$$

$$F.E.M.(ba) = +\frac{wL^2}{12} + \frac{2}{9} PL = +610.1 \text{ kN.m.}$$

$$F.E.M.(ad) = +\frac{wL^2}{2} = +\frac{89.43 * 2.25^2}{2} = +226.37 \text{ kN.m.}$$

Joint	c	a		
member	$c - a$	$a - c$	$a - d$	$a - b$
D.F.	0	0.497	0	0.503
F.E.M.	0	0	+226.37	-610.1
B.M.	0	+190.71	0	+193.02
C.O.M.	+95.35	0	0	0
B.M.	0	0	0	0
M_F	+95.35	+190.71	+226.37	-420.08

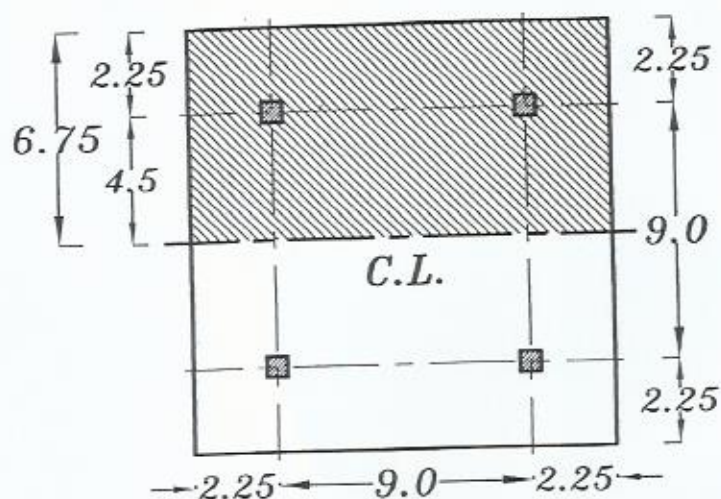


Modification Factor.

عرض شريحه التصميم الكليه

Total Strip width =

$$= \frac{9.0}{2.0} + 2.25 = 6.75 \text{ m}$$



يؤخذ عرض ال
Column strip

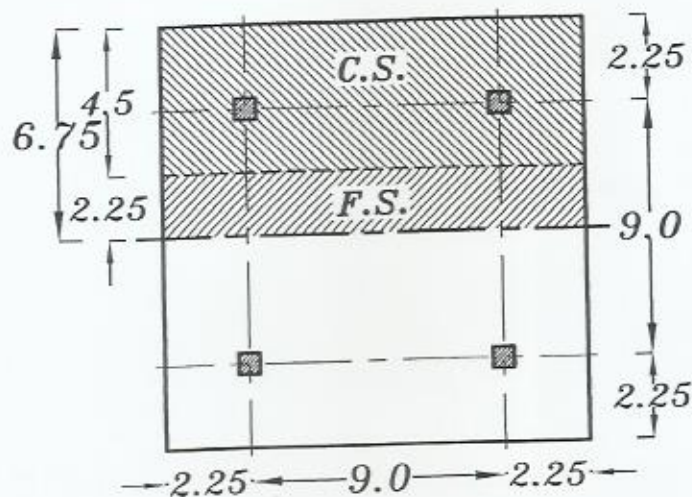
$$b_{C.S.} = \frac{L_2}{4} + \text{Width of the Cantilever}$$

$$b_{C.S.} = \frac{9.0}{4} + 2.25 = 4.50 \text{ m}$$

$$b_{F.S.} = \text{Total Strip width} - b_{C.S.}$$

و يؤخذ عرض ال
Field strip

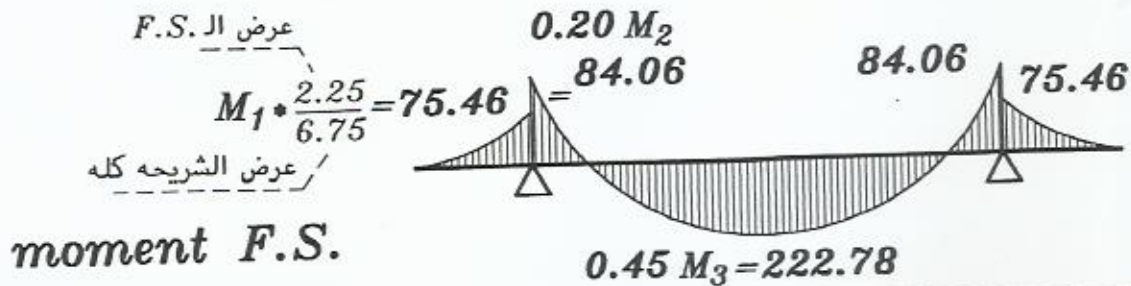
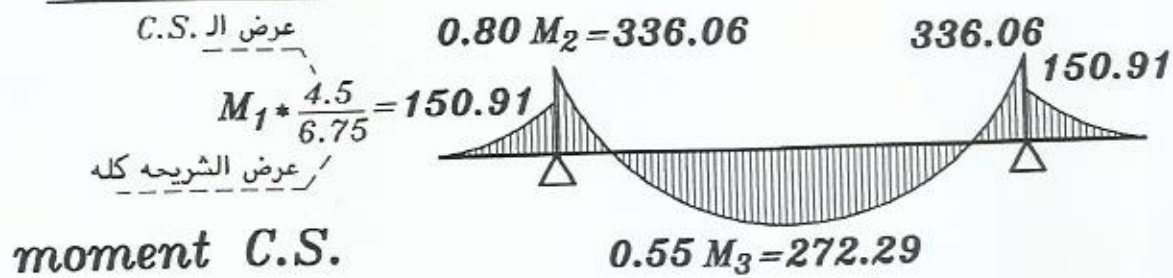
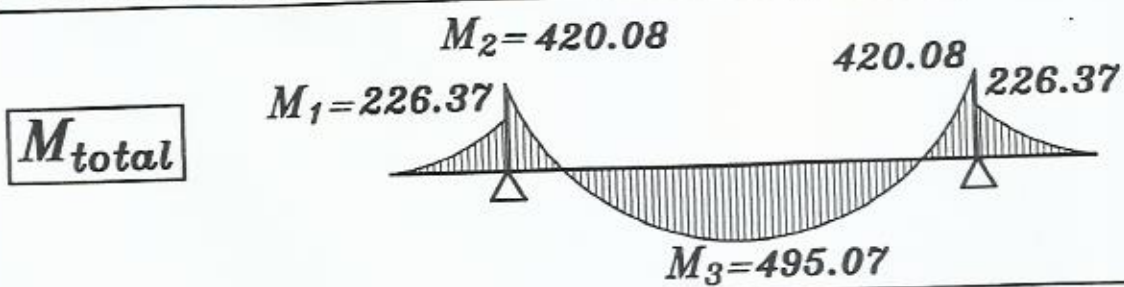
$$b_{F.S.} = 6.75 - 4.5 = 2.25 \text{ m}$$



Modification Factor For Field Strip

$$M.F. = \frac{\text{العرض الحقيقي لل Field strip}}{\frac{1}{4} \text{ عرض الشريحه الكلى}} = \frac{2.25}{3.375} = 0.667$$

Distribute the moment of the Frame
on Column Strip and Field Strip.

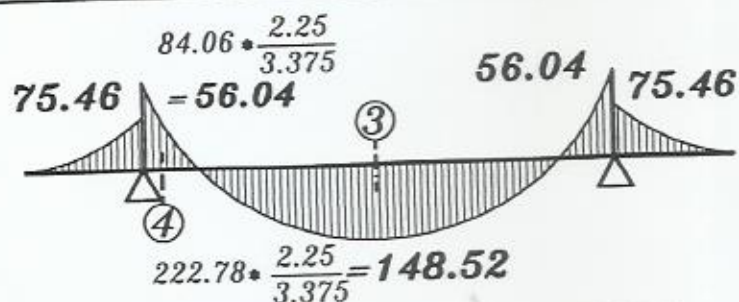


$$\text{Modification Factor} = \frac{2.25}{3.375}$$

$$(M_{F.S.})_{mod.} = (M_{F.S.}) \cdot \text{Modification Factor} = (M_{F.S.}) \cdot \frac{2.25}{3.375}$$

**Modified
moment F.S.**

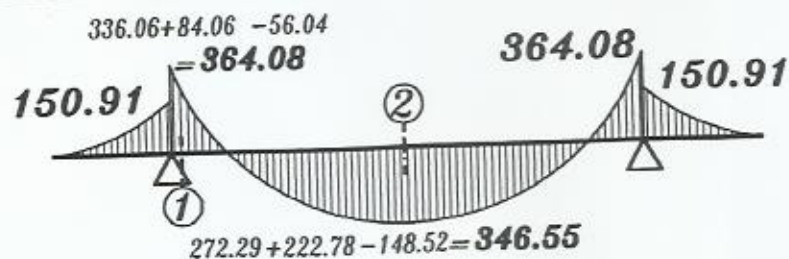
$$b_{F.S.} = 2.25 \text{ m}$$



$$(M_{C.S.})_{mod.} = (M_{C.S.}) + (M_{F.S.}) - (M_{F.S.})_{mod.}$$

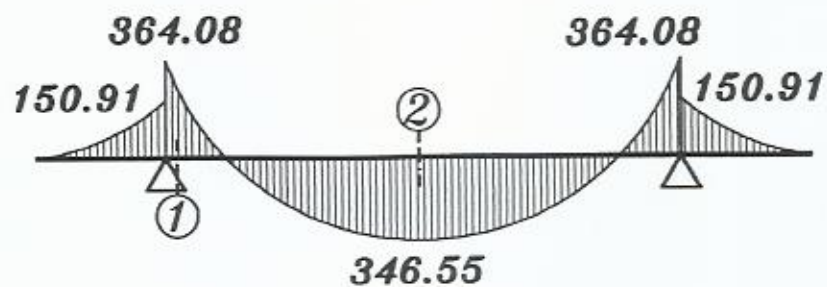
**Modified
moment C.S.**

$$b_{C.S.} = 4.50 \text{ m}$$

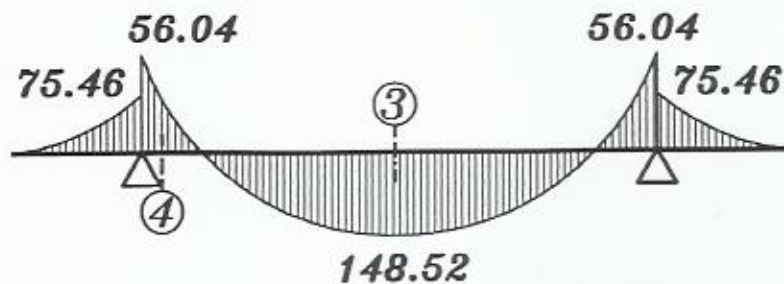


Design the sections of the slab.

Modified
moment C.S.
 $b_{C.S.} = 4.50 \text{ m}$



Modified
moment F.S.
 $b_{F.S.} = 2.25 \text{ m}$

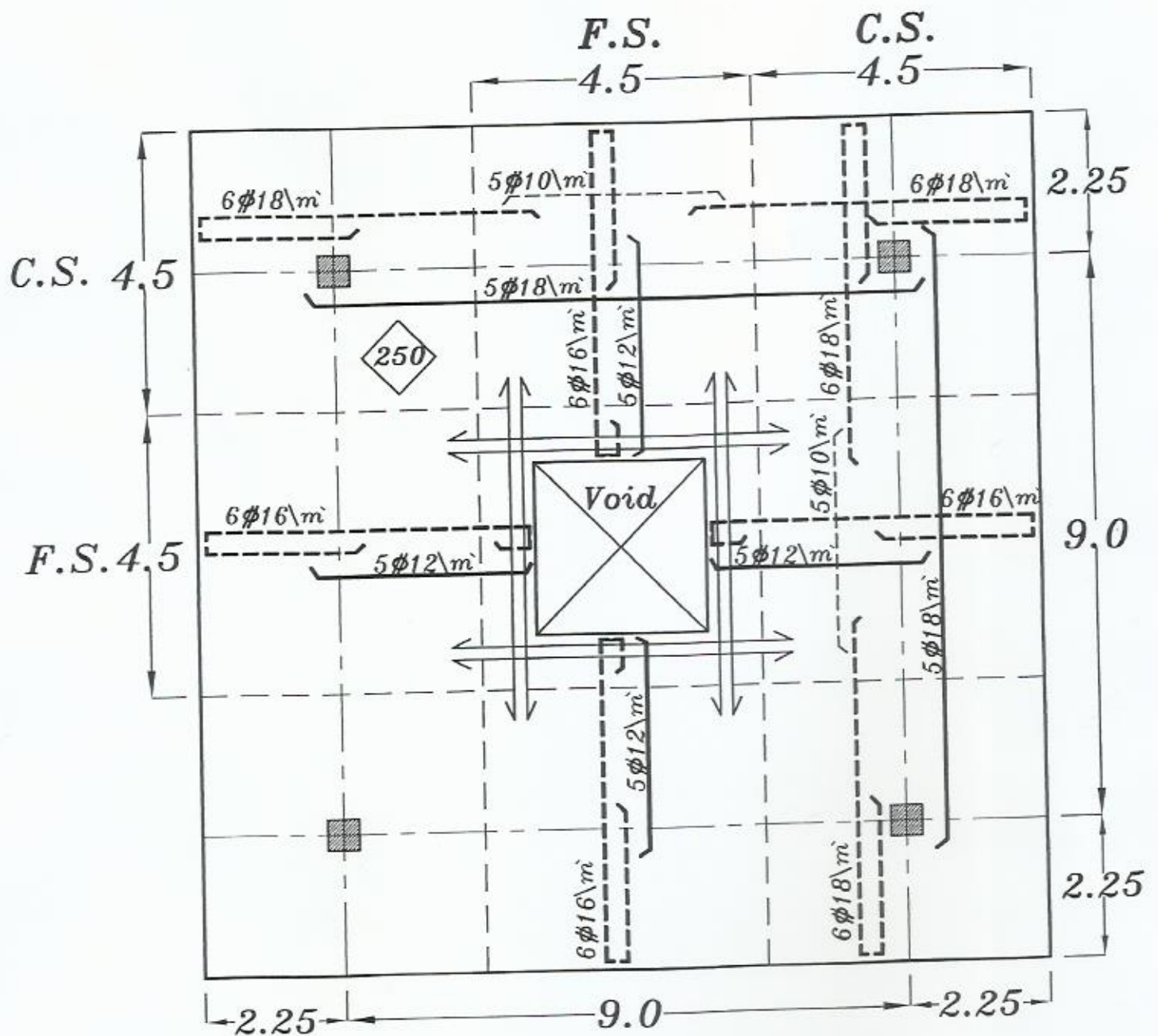


Design of sections.

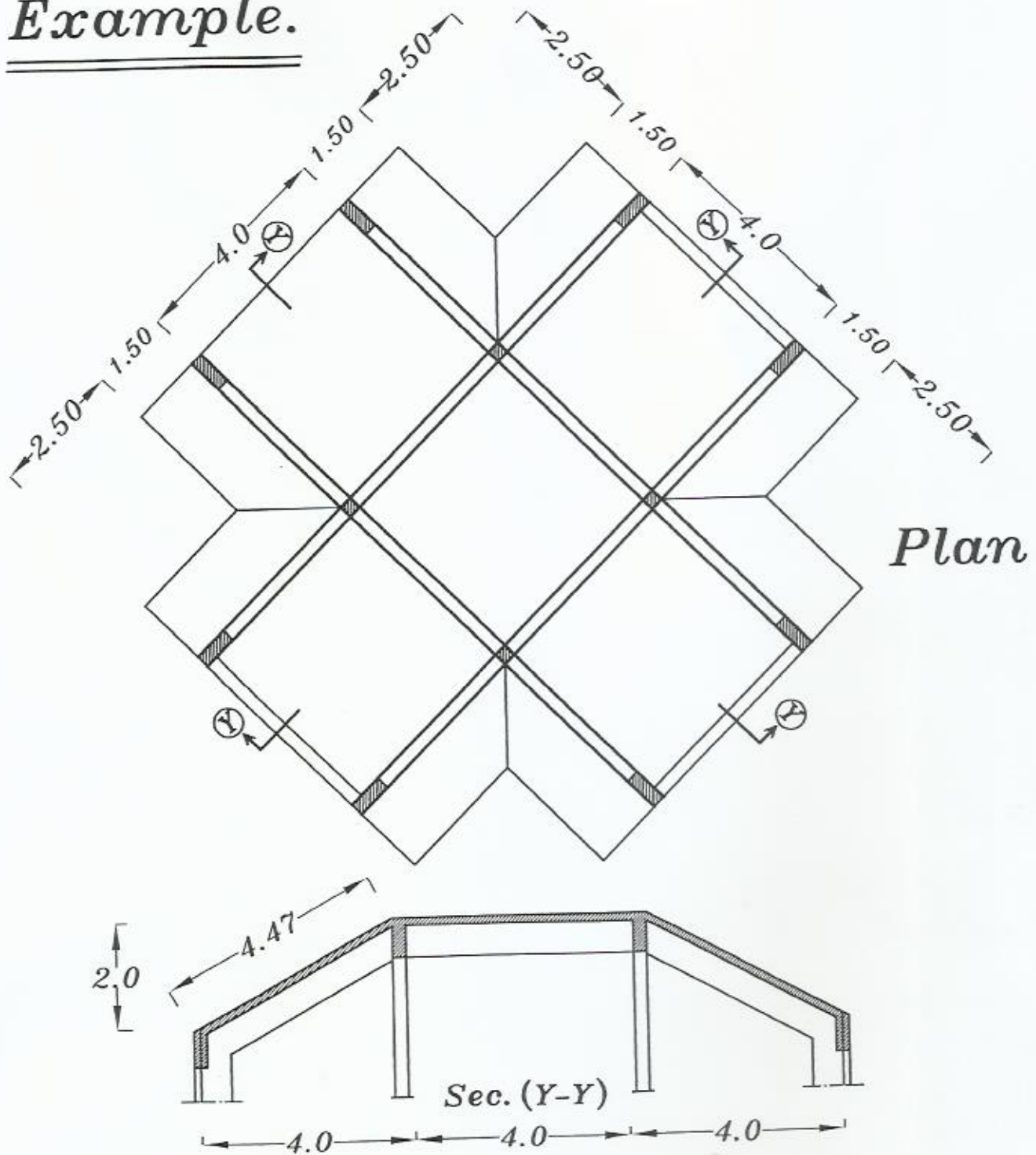
$$d = t_s - 40 \text{ mm} = 250 - 40 = 210 \text{ mm}$$

Strip	Sec.	M (kN.m/strip)	b (m)	d (mm)	C_1	J	A_S (mm ² /b)	A_S (mm ² /m)	No. of bars/m
Column Strip	1	364.08	4500	210	4.04	0.804	5990	1331	6 ϕ 18\m
	2	346.55	4500	210	4.14	0.808	5673	1260	5 ϕ 18\m
Field Strip	3	148.52	2250	210	4.47	0.817	2404	1068	6 ϕ 16\m
	4	56.04	2250	210	7.30	0.826	897	399	5 ϕ 12\m

Details of RFT.



Example.



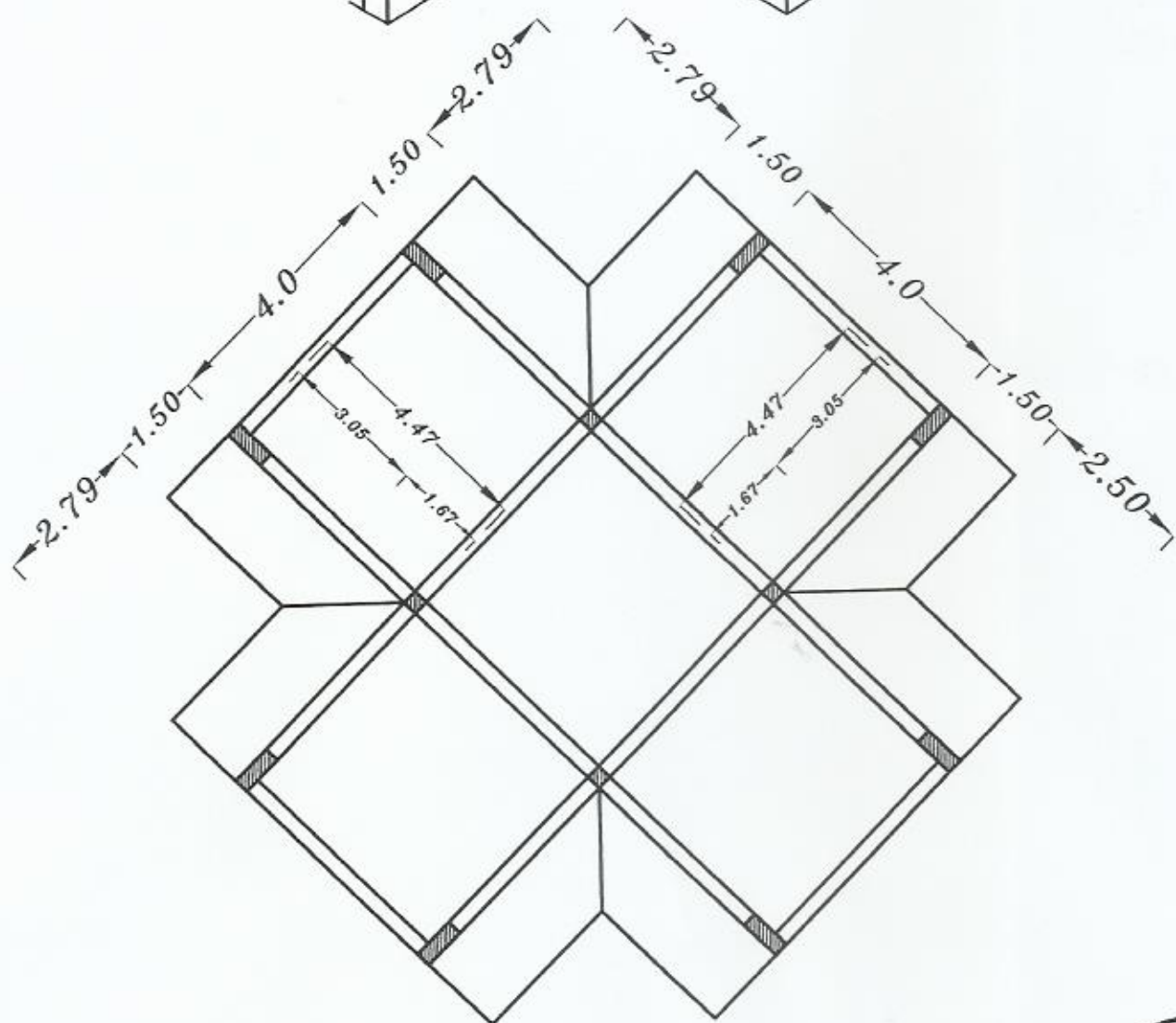
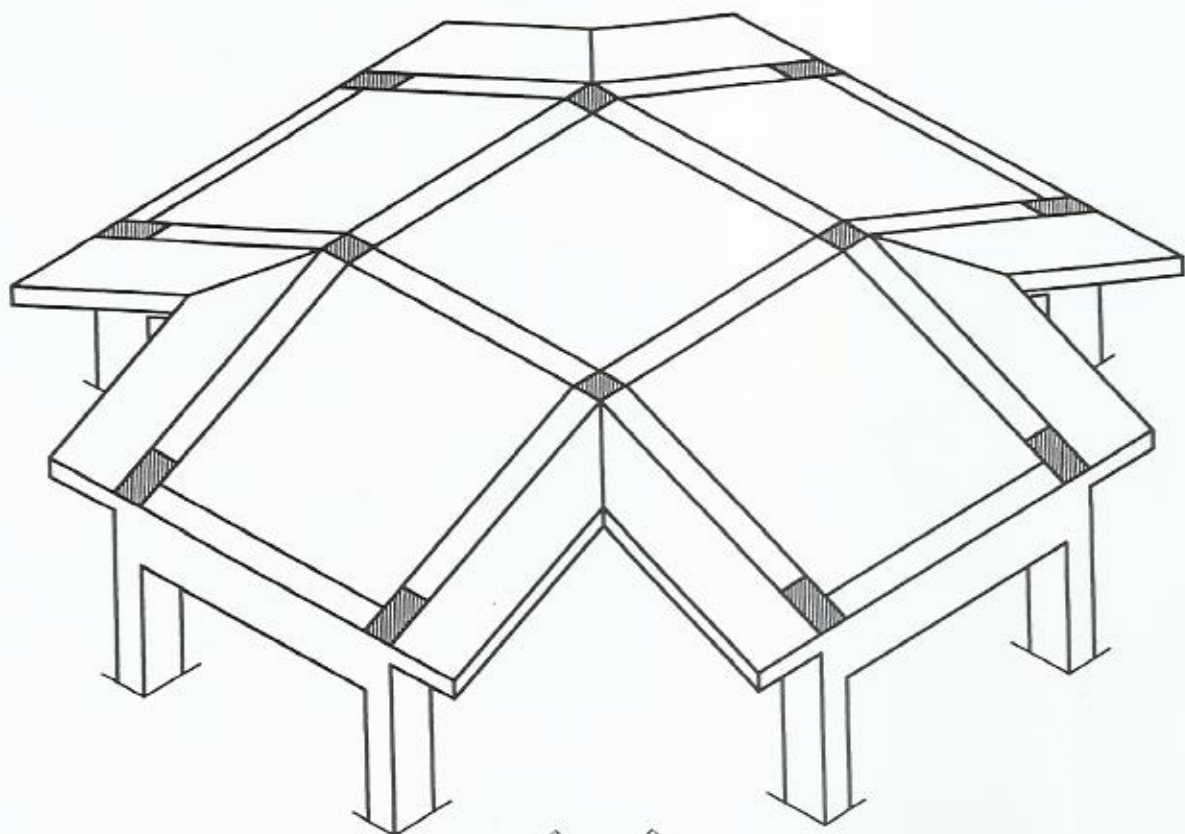
Data.

$$F_{cu} = 25 \text{ N/mm}^2, \quad F_y = 360 \text{ N/mm}^2$$

$$F.C. + L.L. = 2.5 \text{ kN/m}^2 \text{ Horizontal Projection}$$

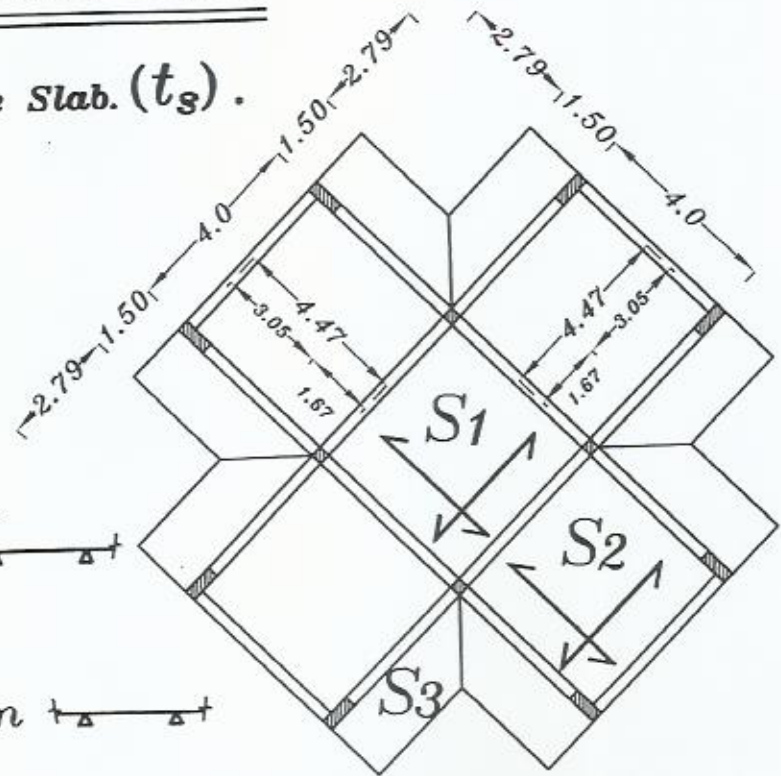
Req.

Design all Slabs & Draw RFT. in plan.



Design the Slabs as Solid Slabs.

a- Choose the Thickness of the Slab. (t_s).



S_1 two way $L_s = 4.0\text{ m}$

$$t_s = \frac{4000}{45} = 88.9\text{ mm}$$

S_2 two way $L_s = 4.0\text{ m}$

$$t_s = \frac{4000}{45} = 88.9\text{ mm}$$

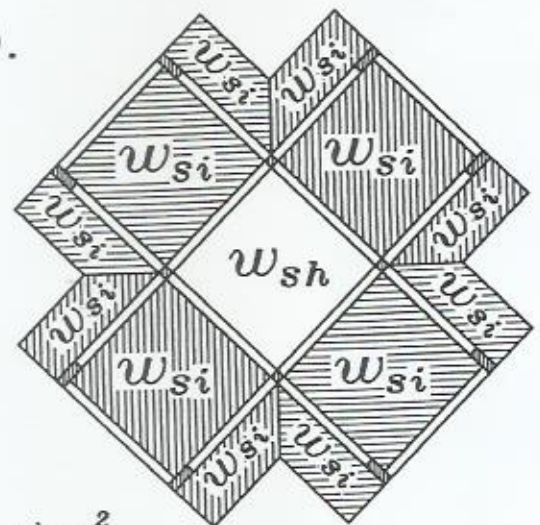
S_3 Cantilever $L_c = 1.5\text{ m}$

$$t_s = \frac{1500}{10} = 150\text{ mm}$$

Take (t_s) the bigger value

$$t_s = 150\text{ mm}$$

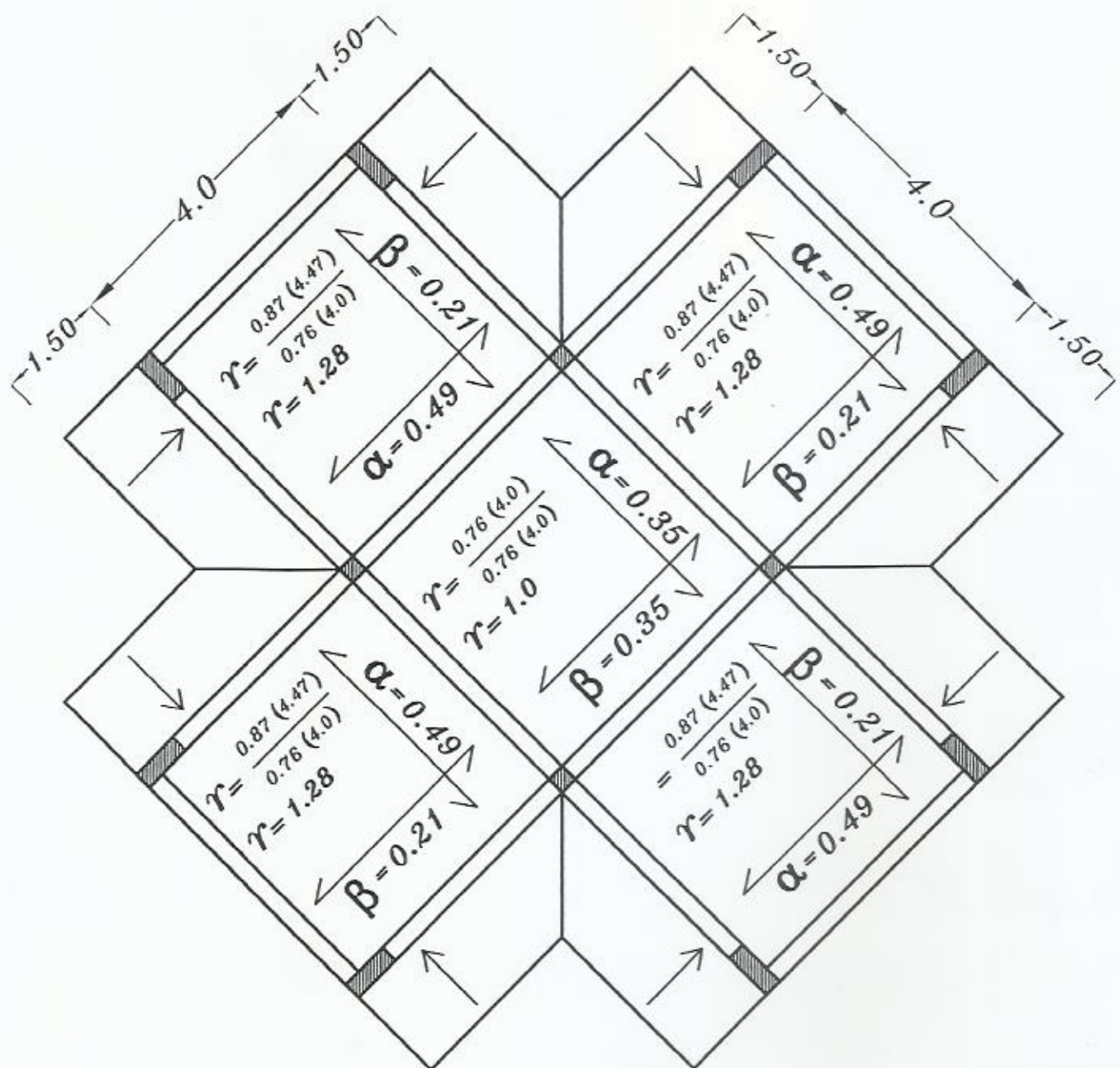
b- Get the Loads on the Slab (w_s).



$$w_{sh} = 1.5 (0.15 * 25 + 2.5) = 9.37\text{ kN/m}^2$$

$$w_{si} = 1.5 (0.15 * 25 + 2.5 * \cos 26.56^\circ) = 8.98\text{ kN/m}^2$$

c- Get the Load Factors α, β

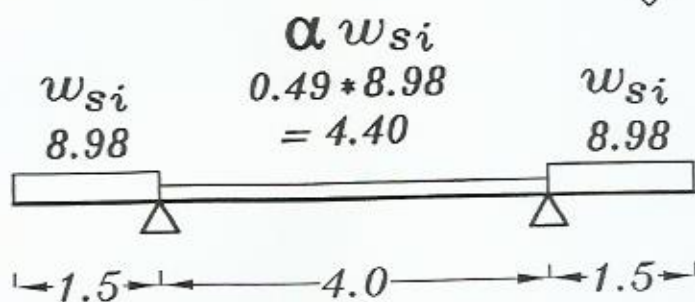
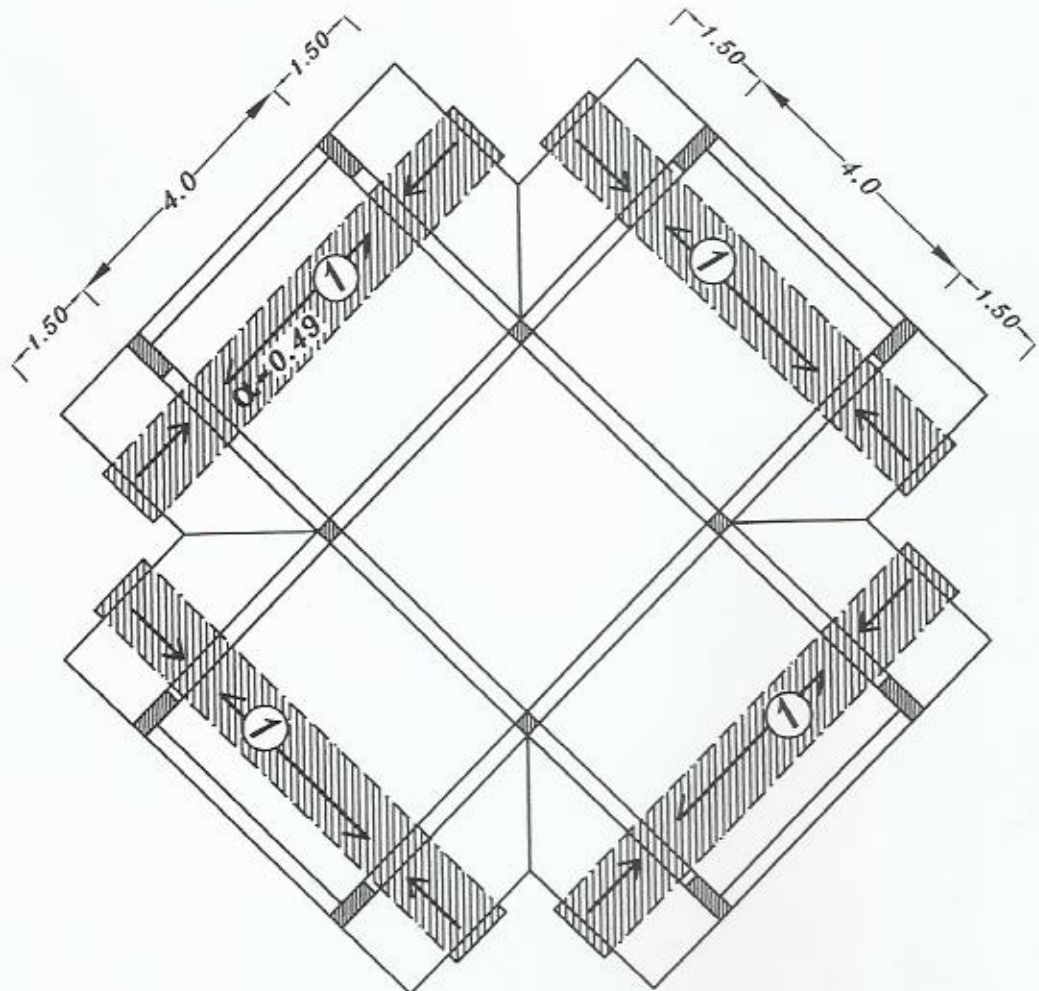


$$\alpha = 0.5 \gamma - 0.15$$

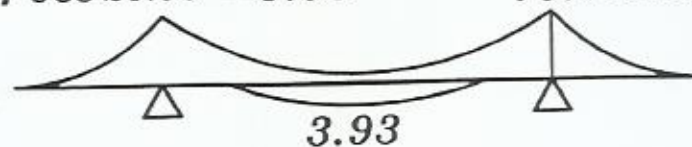
$$\beta = \frac{0.35}{\gamma^2}$$

d- Take a strips in the slab (at the Load direction)
And then Get (B.M.) on the Slab & Design the slab.

Strip ①

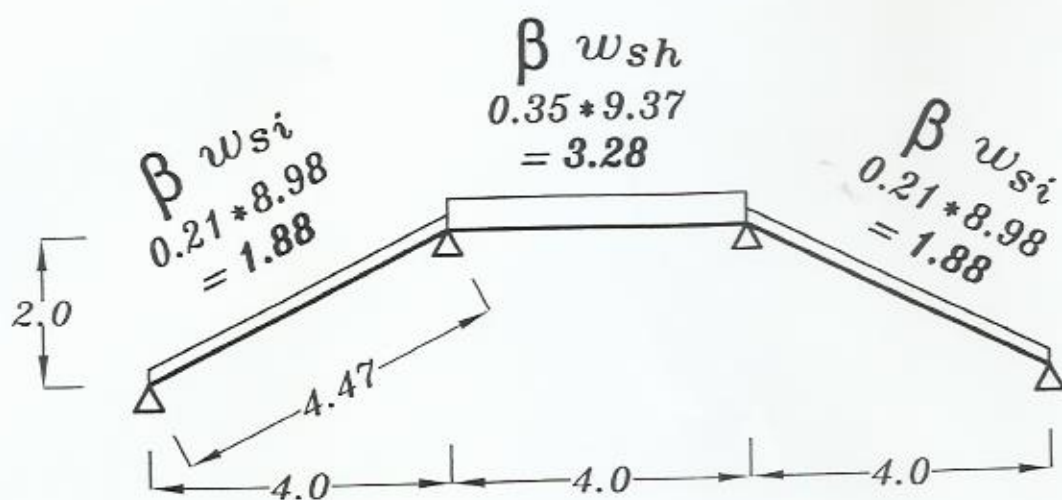
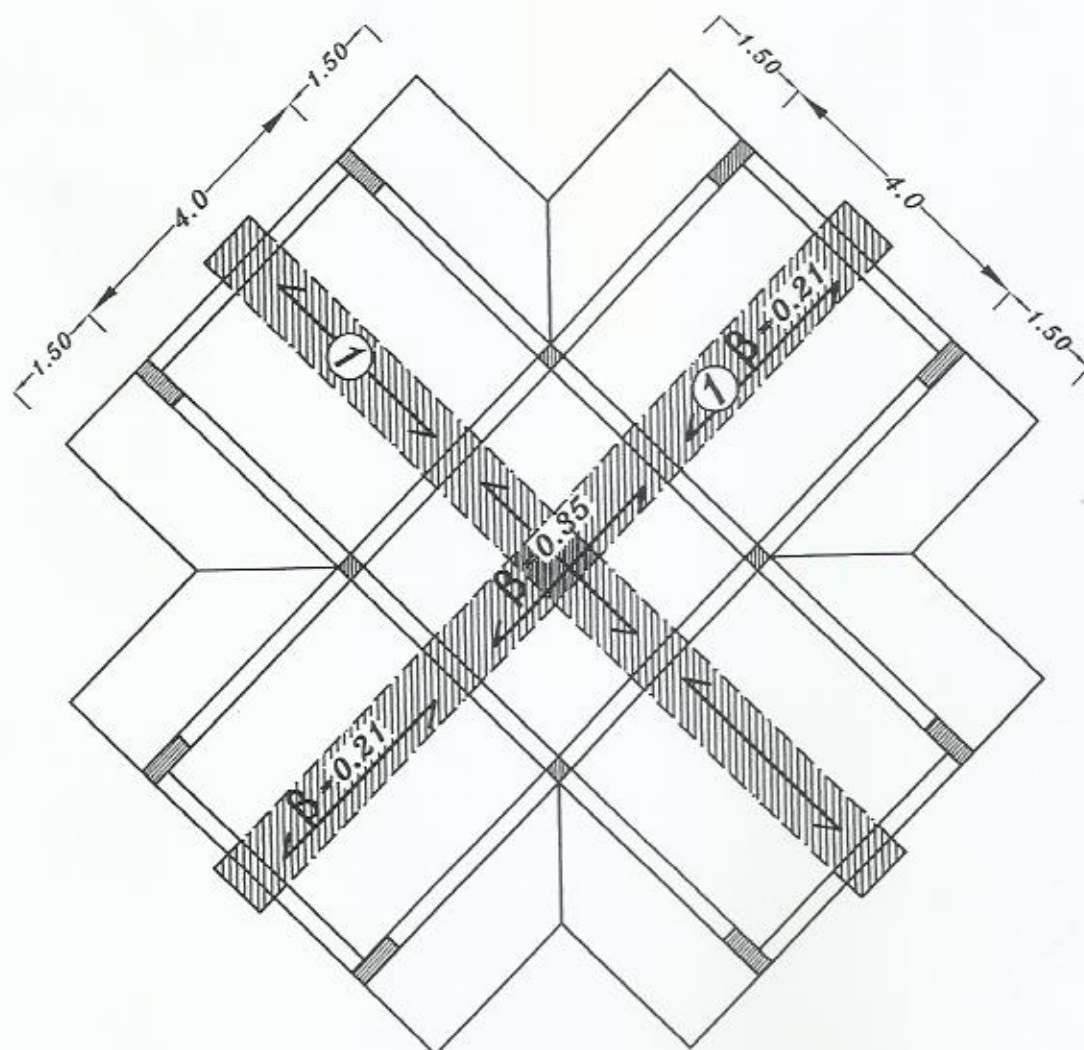


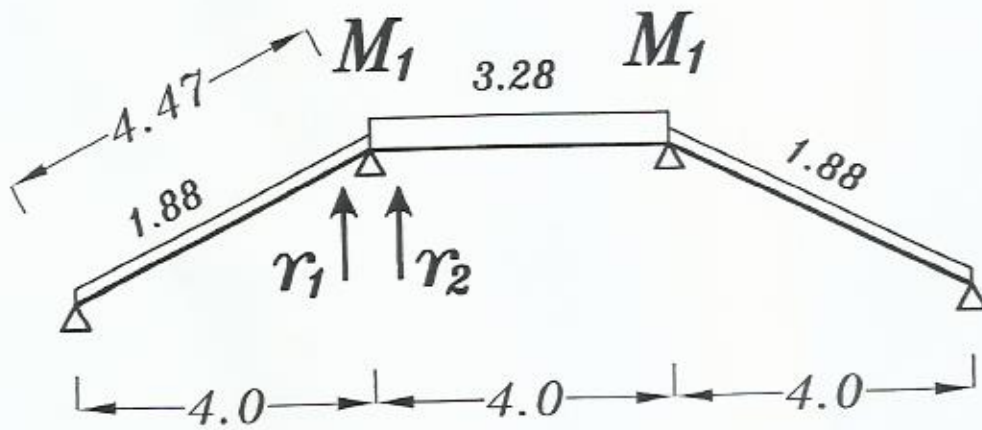
$$10.1 \cos 26.56^\circ = 9.03$$



شريحة أفقيه في بلاطه مائله

Strip ②



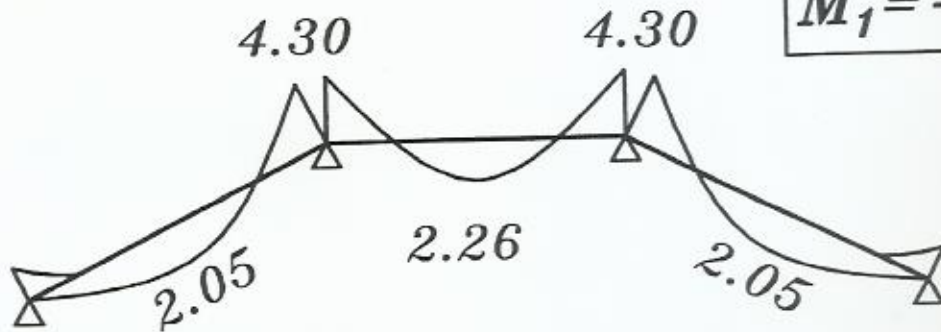


$$\gamma_1 = \frac{wLL^2}{24} = \frac{1.88 \cdot 4.0 \cdot 4.47^2}{24} = 6.26 \quad , \quad \gamma_2 = \frac{wL^3}{24} = \frac{3.28 \cdot 4.0^3}{24} = 8.74$$

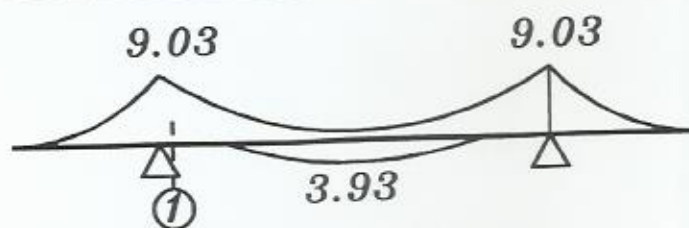
Equation of M_1

$$0.0 + 2M_1(4.47 + 4.0) + M_1(4.0) = -6(6.26 + 8.74)$$

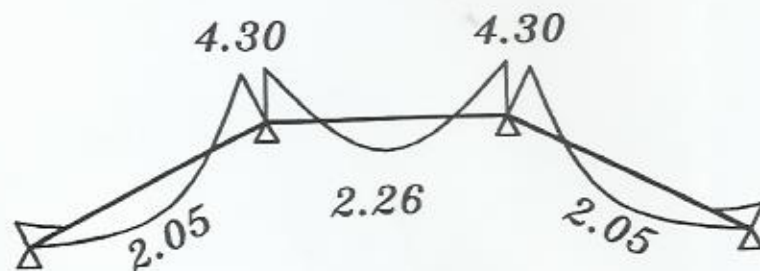
$$M_1 = -4.30 \text{ kN.m.}$$



Strip ①



Strip ②



Sec. ① $M_{U.L.} = 9.03 \text{ kN.m/m}$

عرض الشريحة $t_s = 150 \text{ mm}$, $d = 150 - 20 = 130 \text{ mm}$, $B = 1000 \text{ mm}$

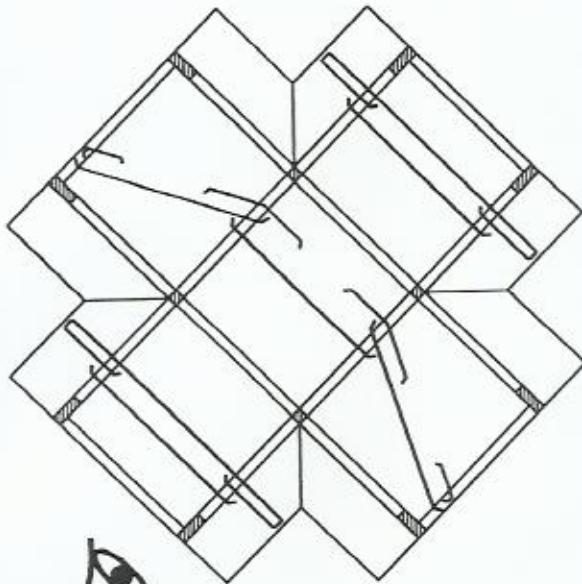
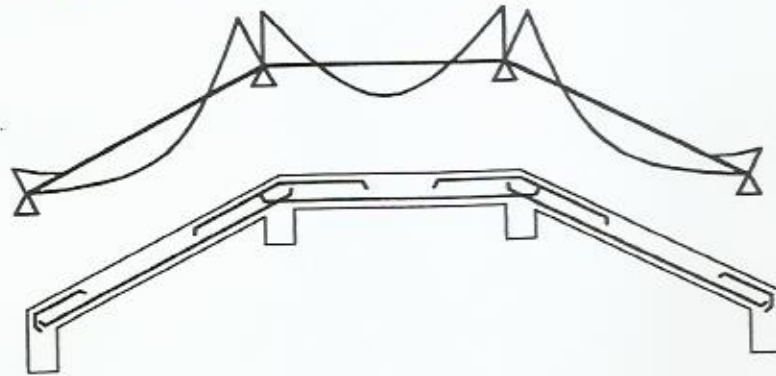
$$130 = C_1 \sqrt{\frac{9.03 \cdot 10^6}{25 \cdot 1000}} \rightarrow C_1 = 6.84 \rightarrow J = 0.826$$

$$A_s = \frac{9.03 \cdot 10^6}{0.826 \cdot 360 \cdot 130} = 235.6 \text{ mm}^2/\text{m}$$

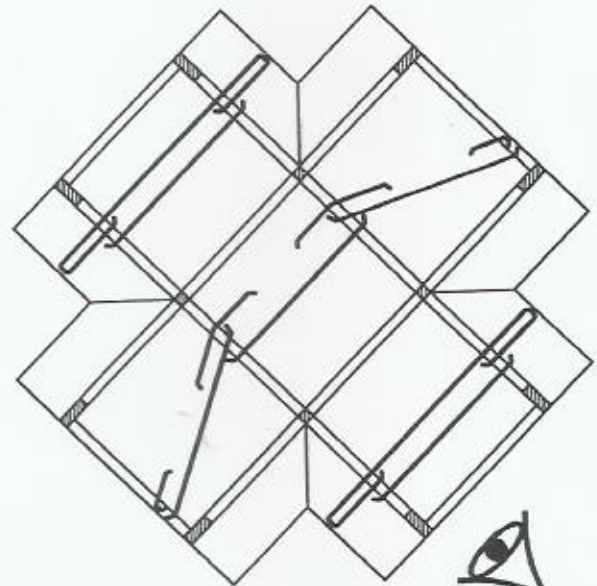
5 ϕ 10\m

∴ سيؤخذ تسليح باقى القطاعات 5 ϕ 10\m

Details of RFT. For the Slab.



نظير بزايه ٤٥°
جهه اليسار



نظير بزايه ٤٥°
جهه اليمين

Details of RFT. For the Slab.

